

Neutrino masses and oscillations

Tests of the Standard Model of Particle Physics II, SS 2020

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(updates by Dr. M. Spalla)

Neutrino (ν) masses and oscillation

- In the Standard Model, neutrinos are massless
 - ν only left-handed ($\bar{\nu}$ only right handed)
 - right handed ν do not participate in the weak interaction
- Neutrino oscillation:
 - first observed in 1998
 - imply that neutrino **must have nonzero mass**
 - as well as violation of lepton flavour conservation, as for quarks

	Mass	m measurements	Discovery
ν_e	< 2 eV	Mainz / Troitsk	Cowan, Reines 1956 (inverse β decay)
ν_μ	< 190 keV	PSI Zürich	Ledermann, Schwartz, Steinberger 1962
ν_τ	< 18.2 MeV	ALEPH (LEP)	DONUT Experiment (FNAL) 2001

Neutrino (ν) masses and oscillation

- Since neutrinos are electrically neutral, they can be either *Dirac spinors* or *Majorana spinors*

- Dirac neutrinos:

- 4 component Dirac spinors: $(\nu_L^D, \bar{\nu}_R^D; \nu_R^D, \bar{\nu}_L^D)$

- With:

$$\bar{\nu}_R^D = \text{CPT}(\nu_L^D) , \quad \bar{\nu}_L^D = \text{CPT}(\nu_R^D)$$

- Majorana neutrinos:

- 2 component Majorana spinors: $(\nu_L^M; \nu_R^M)$

- Majorana neutrinos are their own antiparticle:

$$\bar{\nu}_R^M = \text{CPT}(\nu_L^M) \equiv \nu_R , \quad \bar{\nu}_L^M = \text{CPT}(\nu_R^M) \equiv \nu_L$$

- Which of the two occurs in nature is yet to be clarified experimentally
- The very low value of the neutrino mass is also yet to be theoretically explained

Mechanism of ν oscillation

- The same argument discussed for quarks also holds for neutrino
 - From interaction with Higgs field
- ν mass eigenstates \neq ν weak eigenstates
 - Mass matrix is non-diagonal on the weak eigenstates basis
 - Same applies to charged leptons, known to have nonzero (and very different) masses
- It follows that weak transitions exist between mass states in different generations: ν mixing
 - Time oscillation between mixing states as for neutral mesons
 - First: Bruno Pontecorvo, Moscow 1958

Mechanism of ν oscillation

- As for quarks, both up-type (neutral) and down-type (charged) lepton weak eigenstates are connected to the mass eigenstates by a unitary transform

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}_L = U_u \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}_L = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}_L$$

$$\begin{aligned} \nu_i \quad (i = 1, \dots, 3) \\ \nu_\alpha \quad (\alpha = e, \mu, \tau), \end{aligned} \quad \Rightarrow \quad \left\{ \begin{aligned} \nu_i &= \sum_{\alpha} U_{\alpha i}^* \nu_{\alpha} ; & \bar{\nu}_i &= \sum_{\alpha} U_{\alpha i} \bar{\nu}_{\alpha} ; \\ \nu_{\alpha} &= \sum_i U_{\alpha i} \nu_i ; & \bar{\nu}_{\alpha} &= \sum_i U_{\alpha i}^* \bar{\nu}_i . \end{aligned} \right.$$

Mechanism of ν oscillation

- U_ν is the Pontecorvo-Maki-Nakagawa-Sakata mixing matrix:

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ \cdot \begin{pmatrix} e^{i\phi_1} & 0 & 0 \\ 0 & e^{i\phi_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Independent parameters:

- **3** mixing angles:

$$\theta_{ij} \quad (i, j = 1, 2, 3; i > j),$$

$$c_{ij} = \cos \theta_{ij} > 0,$$

$$s_{ij} = \sin \theta_{ij} > 0,$$

- **1** CP-violating phase:

$$e^{i\delta}$$

- **2** Majorana phases:

$$\phi_1, \phi_2 \quad (\nu^M \equiv \bar{\nu}^M \text{ for Majorana neutrino})$$

► Majorana phases play no role in oscillation

Mechanism of ν oscillation

- Time evolution of weak eigenstate:

$$\nu_i(t) = e^{-iE_i t} \nu_i(0) ,$$

- In the limit $|\vec{p}| \gg m_i$ (ν have very small masses)

$$E_i = \sqrt{\vec{p}^2 + m_i^2} \stackrel{m_i \ll |\vec{p}|}{\approx} |\vec{p}| + \frac{1}{2} \frac{m_i^2}{|\vec{p}|} \stackrel{|\vec{p}| \approx E_\nu}{\approx} E_\nu + \frac{1}{2} \frac{m_i^2}{E_\nu} .$$

- We can then derive the time evolution of a weak eigenstate:

$$|\nu(0)\rangle = |\nu_\alpha\rangle = \sum_i U_{\alpha i} \nu_i(0) ,$$

$$\Rightarrow \nu(t) = \sum_i U_{\alpha i} e^{-iE_i t} \nu_i(0) = \sum_i \sum_\beta U_{\alpha i} U_{\beta i}^* e^{-iE_i t} \nu_\beta .$$

Mechanism of ν oscillation

- From $\nu(t)$ time evolution, the transition probability from weak state α to weak state β can be derived:

$$\begin{aligned} \mathcal{P}(\nu_\alpha \rightarrow \nu_\beta; t) &= |\langle \nu_\beta | \nu(t) \rangle|^2 \\ &= \sum_i |U_{\alpha i} U_{\beta i}^*|^2 + 2\text{Re} \sum_{i,j(j>i)} U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j} e^{-i\Delta_{ij}}, \end{aligned}$$

- Where ($L = ct$):

$$\Delta_{ij} = (E_i - E_j)t \approx \frac{m_i^2 - m_j^2}{2E}t =: \frac{1}{2} \underline{\underline{\Delta m_{ij}^2}} \frac{L}{E}.$$

- Nonzero oscillation means nonzero $\Delta m_{ij}^2 = m_i^2 - m_j^2$
 - The ν masses are not all identical and cannot be all = 0
 - Otherwise the mass matrix would have been a multiple of \mathbb{I} and there wouldn't have been any mixing

Mechanism of ν oscillation

- Simplest case: mixing between two generations
 - 1 parameter: mixing angle θ

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

- Transition probabilities:

$$\begin{aligned} \mathcal{P}(\nu_e \rightarrow \nu_e) &= \mathcal{P}(\nu_\mu \rightarrow \nu_\mu) = \mathcal{P}(\bar{\nu}_e \rightarrow \bar{\nu}_e) = \mathcal{P}(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu) \\ &= 1 - \sin^2 2\theta \sin^2 \frac{\Delta}{2} \\ \mathcal{P}(\nu_e \rightarrow \nu_\mu) &= \mathcal{P}(\nu_\mu \rightarrow \nu_e) = \mathcal{P}(\bar{\nu}_e \rightarrow \bar{\nu}_\mu) = \mathcal{P}(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \\ &= \sin^2 2\theta \sin^2 \frac{\Delta}{2} = 1 - \mathcal{P}(\nu_e \rightarrow \nu_e), \end{aligned}$$

With: $\Delta = \frac{\Delta m^2 L}{2E} \quad \Rightarrow \quad \text{Oscillation length: } L_0 = \frac{4\pi E}{\Delta m^2}.$

Mechanism of ν oscillation

- Simple case of 2 families

$$\begin{aligned} \mathcal{P}(\nu_e \rightarrow \nu_e) &= \mathcal{P}(\nu_\mu \rightarrow \nu_\mu) = \mathcal{P}(\bar{\nu}_e \rightarrow \bar{\nu}_e) = \mathcal{P}(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu) \\ &= 1 - \sin^2 2\theta \sin^2 \frac{\Delta}{2} \end{aligned}$$

$$\mathcal{P}(\nu_e \rightarrow \nu_\mu) = \mathcal{P}(\nu_\mu \rightarrow \nu_e) = \mathcal{P}(\bar{\nu}_e \rightarrow \bar{\nu}_\mu) = \mathcal{P}(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$$

$$\Delta = \frac{\Delta m^2 L}{2 E}$$

$$= \sin^2 2\theta \sin^2 \frac{\Delta}{2} = 1 - \mathcal{P}(\nu_e \rightarrow \nu_e),$$

- Transition probabilities depend on 2 parameters:
 - oscillation amplitude: $\sin^2 2\theta$
 - oscillation frequency: $\Delta m^2 / 2E_\nu$
- For 3 generations, complex mixing matrix U_ν parametrised as for CKM
 - CP violation becomes possible: $\mathcal{P}(\nu_e \rightarrow \nu_\mu) \neq \mathcal{P}(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$
 - ▶ But CPT requires that: $\mathcal{P}(\nu_e \rightarrow \nu_\mu) \equiv \mathcal{P}(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$

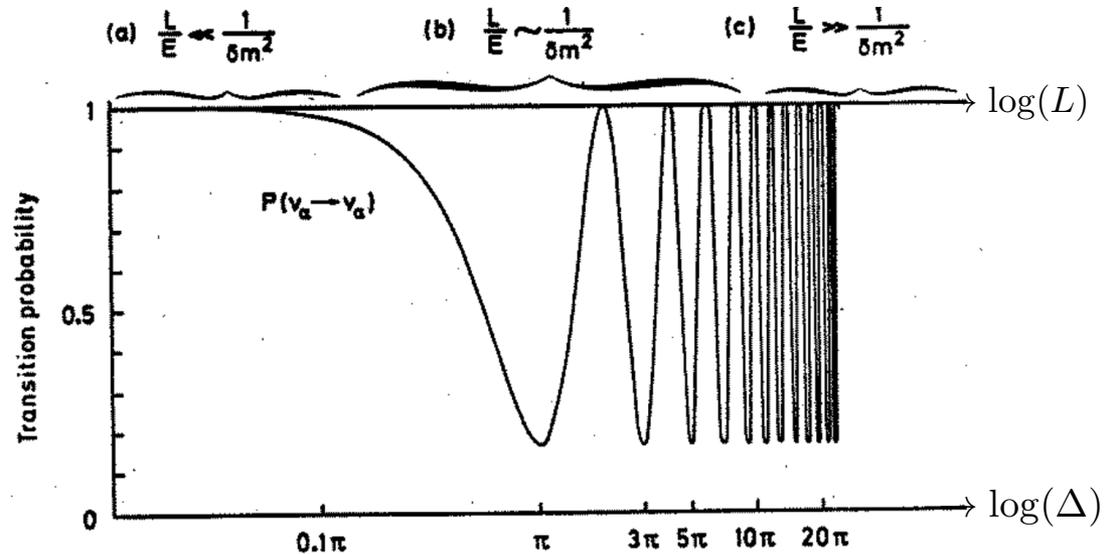
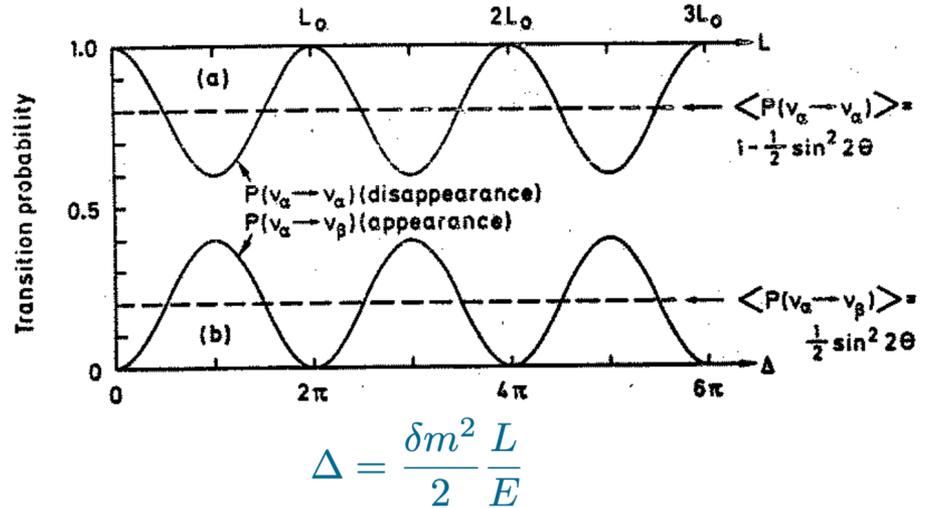
Sensitivity to ν oscillation

$$L_0 = \frac{4\pi E}{\delta m^2}$$

- Sensitivity to a given δm^2 depends on L/E
 - i.e. the energy of the produced ν and the distance between source and detector

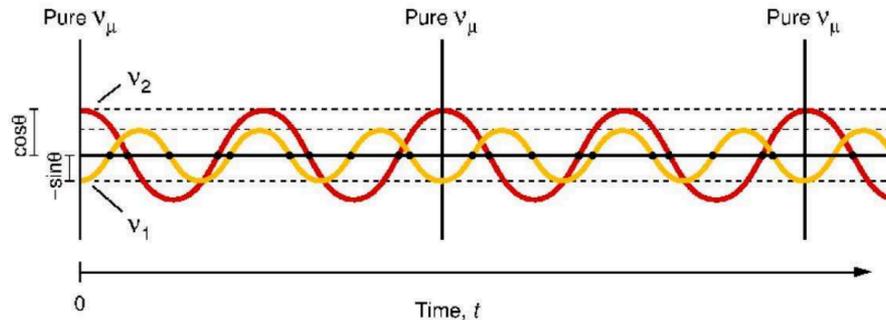
- Optimal sensitivity when the oscillation frequency is neither too large nor too small:

$$\frac{L}{E} \sim \frac{1}{\delta m^2}$$



Note about charged leptons

- Oscillation is a pure quantum mechanical effect: coherent superposition of ν mass eigenstates



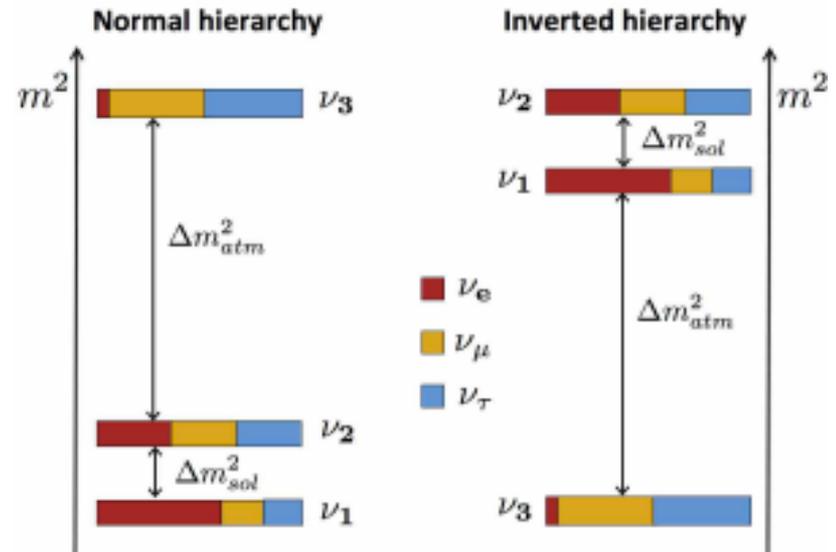
- It is visible only because momentum resolution doesn't allow us to resolve the mass eigenstates
 - i.e. the oscillation length L_0 is long enough
- In charged leptons and quarks, masses can be resolved and the effect is disrupted
 - To resolve the mass states, it must be: $\Delta p < |p_i - p_j|$
 - Hence L_0 is smaller than spatial resolution:

$$L_0 = \frac{4\pi E}{\delta m^2}.$$

$$\Delta x > \frac{1}{\Delta p} > \frac{1}{|p_i - p_j|} \approx \frac{2E}{|m_i^2 - m_j^2|} \approx L_0^{ij},$$

What can we learn from ν oscillation?

- ν mass differences: ordering of the ν_i mass states
 - The absolute scale of ν mass cannot be measured from oscillation: direct measurement needed
- Mixing angles
 - Built a ‘unitarity triangle’ for leptons
- CP violating phase: CP violation in lepton mixing?



Search for ν oscillation

- Typical ν experiment

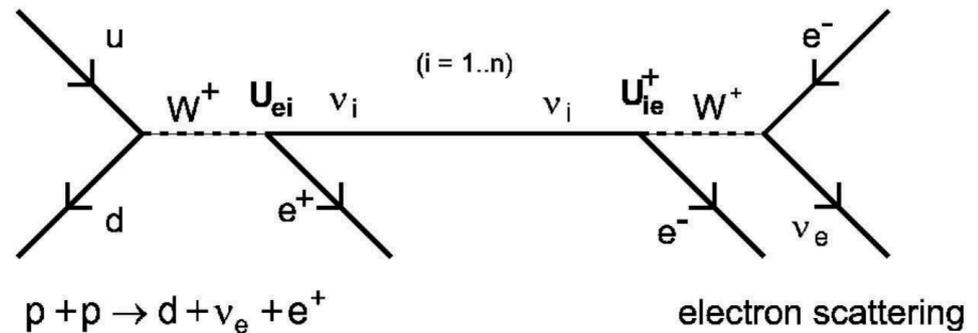
- A source creates ν of a specific flavour ν_α in a given energy range, at $t=0$
- A detector then measures the flavour components of the ν flux at time $t=L/c$:

$$\nu(t) = \sum_{i,\beta} U_{\alpha i} U_{\beta i}^* e^{-iE_i t} |\nu_\beta \rangle$$

► as well as the neutrino's energy

- The distance L between source and detector tuned in order to be sensitive to the δm^2 of interest

Example:



- Two classes of experiments: **appearance and disappearance experiments**

Disappearance experiments

- Detector sensitive to same flavour as produced in the source
- Measuring the ν_α flux (ν rate / detector area) in the detector as a function of ν energy

- Survival probability: $\mathcal{P}(\nu_\alpha \rightarrow \nu_\alpha; L)$

- equivalent to measuring the probability of oscillation into **any other** flavour eigenstate

$$\mathcal{P}(\nu_\alpha \rightarrow \nu_X \neq \nu_\alpha; L) \equiv 1 - \mathcal{P}(\nu_\alpha \rightarrow \nu_\alpha; L)$$

- Requires:
 - precise knowledge of the source or
 - measurements at multiple distances

Appearance experiments

- Detection of a different flavour than that generated at the source
- Measures the probability of appearance of a specific flavour

$$\mathcal{P}(\nu_\alpha \rightarrow \nu_\beta; L).$$

- Requires
 - low contamination of the source with ν_β or
 - precise knowledge of source flavour composition

Sensitivity to ν oscillation

- The fundamental parameter is the oscillation frequency
 - For each oscillation component

$$S := \sin^2 \frac{\Delta}{2} = \sin^2 \left[\frac{\Delta m^2 L}{4E} \right]$$

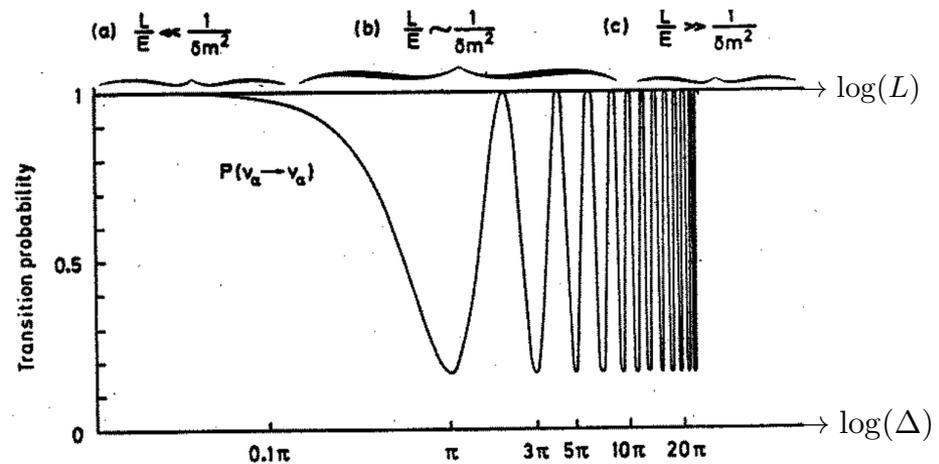
- Three ranges can be considered:

1. $L/E \ll 4/\Delta m^2$

(or $L \ll L_0 = 4\pi E / \Delta m^2$)

$\Rightarrow S \approx 0$

- No sensitivity to oscillation



Sensitivity to ν oscillation

2. $L/E \geq 4/\Delta m^2$

- At sensitivity threshold: *condition on* minimum Δm^2 the experiment is sensitive to (given L and E)

- Large L and low E improve sensitivity to small Δm^2

$$\Delta m_{\min}^2 \approx \frac{E \text{ [MeV]}}{L \text{ [m]}} \text{ eV}^2$$

- But ν flux decreases with distance (isotropic, divergent beam)

3. $L/E \gg 4/\Delta m^2$ (or $L \ll L_0$)

- High frequency: many oscillations between source and detector
- L/E must be measured very precisely to resolve oscillations
- Otherwise it is only possible to observe average transition probability
- i.e. measure θ but not Δm^2

$$\langle \mathcal{P}(\alpha \rightarrow \beta \neq \alpha) \rangle = \frac{1}{2} \sin^2 \theta$$

○ L/E determines the mass range to which the experiment is sensitive

- i.e. basic parameter in order to decide what experiment should be built to test a given Δm^2 region

Types of ν sources

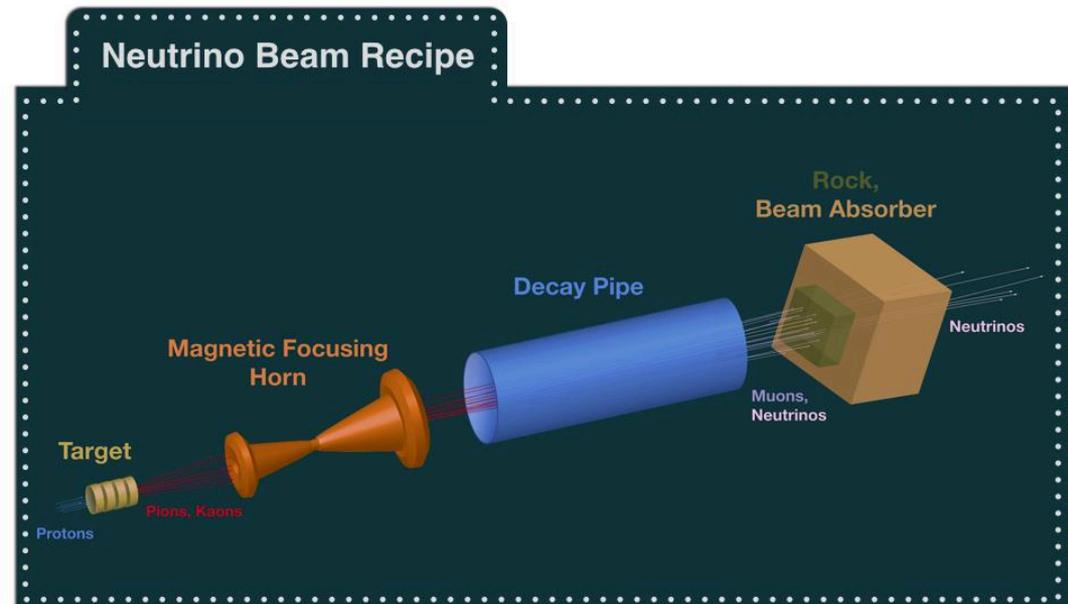
Experiment	L (m)	E (MeV)	$ \Delta m^2 $ (eV ²)	Produced flavour
Solar	10^{10}	1	10^{-10}	ν_e
Atmospheric	$10^4 - 10^7$	$10^2 - 10^5$	$10^{-1} - 10^{-4}$	$\nu_\mu, \bar{\nu}_\mu, \nu_e, \bar{\nu}_e$
Reactor	SBL $10^2 - 10^3$	1	$10^{-2} - 10^{-3}$	$\bar{\nu}_e$
	LBL $10^4 - 10^5$		$10^{-4} - 10^{-5}$	
Accelerator	SBL 10^2	$10^3 - 10^4$	> 0.1	$\nu_\mu, \bar{\nu}_\mu$
	LBL $10^5 - 10^6$	$10^3 - 10^4$	$10^{-2} - 10^{-3}$	

SBL = short baseline, LBL = long baseline (see next)

- Neutrinos from supernovas have also been measured, but they are used as messengers for astronomy research rather than for studying neutrino properties

Neutrino beams

- **Nuclear reactors:** ν from β decays in the fission process
 - Produces low energy $\bar{\nu}_e$
 - Needs detailed knowledge of neutrino flux produced by the reactor (many decay chains involved)
- **Accelerators:**
 - proton beam on fixed target
 - interaction with nuclei in target produces π, K
 - ν from π, K *weak decays*
 - Produces $\nu_\mu, \bar{\nu}_\mu$, energy can be tuned



Neutrino beams: detection

- Detection method: mostly inverse β decay



- Decay products then detected through

- electron-positron annihilation: $e^+e^- \rightarrow \gamma\gamma$ Prompt photon
- neutron capture: $n + p \rightarrow d + \gamma$ 2.2 MeV $n + Gd \rightarrow Gd^* \rightarrow Gd + \gamma$ 8 MeV
- ▶ Often use Gadolinium (Gd) for high neutron capture efficiency
- Photons can be detected



- Then detect charged lepton (e.g. through Cherenkov light)
 - Charged leptons retains ν direction and energy (forward scattering)
- For better precision, two detectors are often used (multi-detector):
 - One near the source, to measure the produced flux
 - One at distance, to detect oscillations

Neutrino beams: measurements

○ Reactors:

- Only disappearance measurements
 - Direct detection of ν_μ, ν_τ from oscillation is not possible due to low energy: under threshold for producing a μ/τ
- $\bar{\nu}_e$ disappearance: address $\nu_e \rightarrow \nu_\tau / \nu_\mu$ oscillation (same as solar neutrinos)

○ Accelerators:

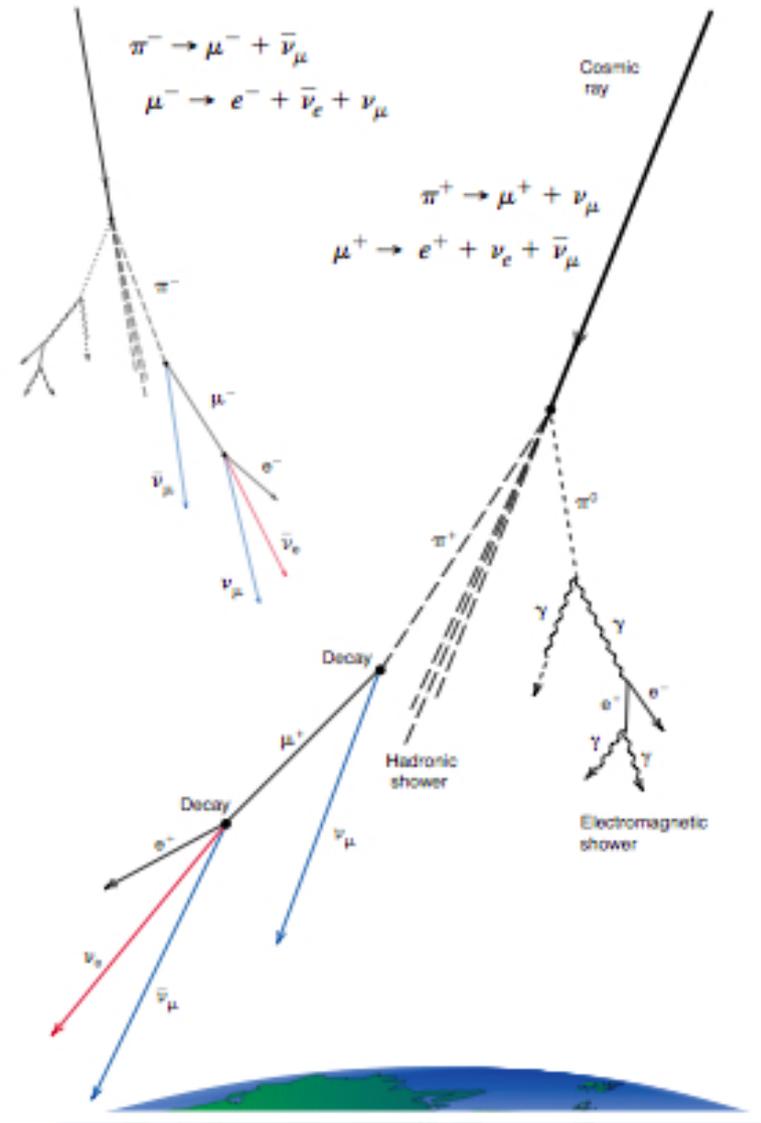
- ν_μ disappearance, ν_τ/ν_e appearance
- can verify $\nu_\mu \rightarrow \nu_\tau$ oscillation observed in atmospheric neutrino (see next)
- and target $\nu_\mu \rightarrow \nu_e$ observation

Neutrino beams: long baseline vs short baseline

- Two categories:
 - **Short baseline**: distance between source and detector up to 100-1000 m
 - **Long baseline**: distance between source and detector > 100 Km
- Designed to address different ranges in Δm^2
 - For instance: $\Delta m^2 = \mathcal{O}(10^{-3})$ eV (observed in atmospheric neutrinos)
 - ▶ First oscillation maximum at $L/E \sim 500$ km/GeV
 - ▶ e.g. accelerator neutrinos produced at \sim GeV \rightarrow need $L \sim 10^3$ Km

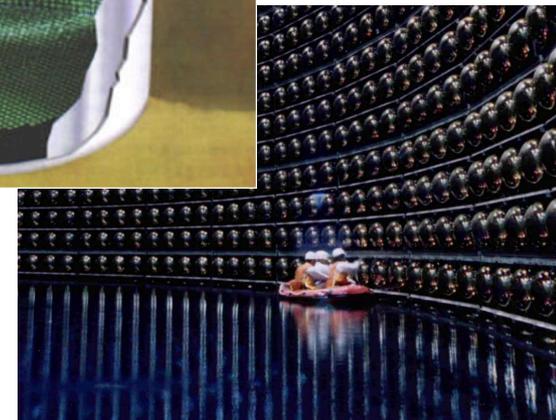
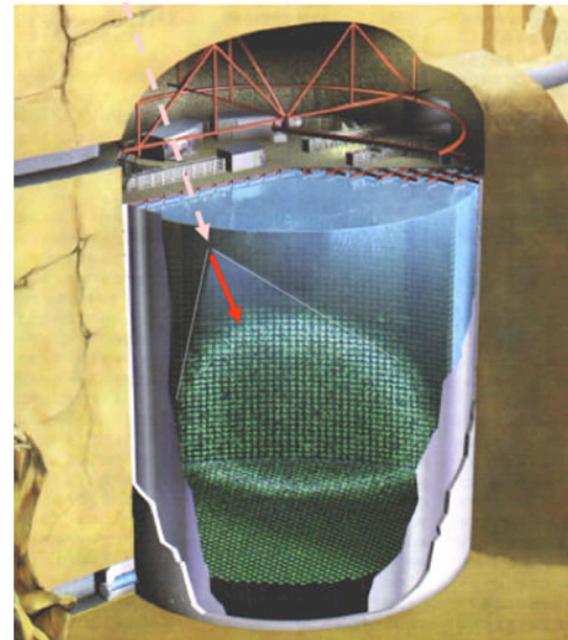
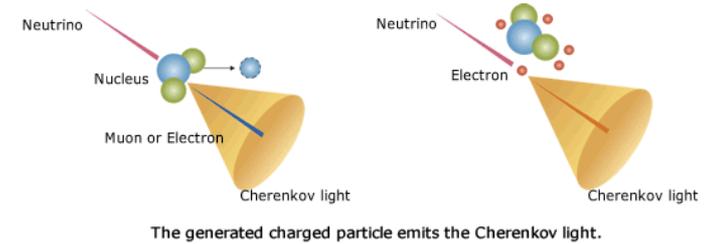
Atmospheric neutrinos

- Cosmic radiation ($\sim 99\%$ protons) interacts with atoms in the atmosphere
 - Produces particle showers: π , K produce ν by decaying weakly
- Oscillation observed for the first time in atmospheric ν by [Superkamiokande](#) experiment
 - 1998



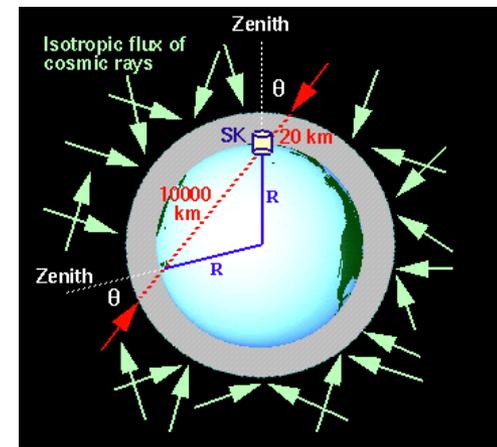
Superkamiokande experiment

- 5000 ton water tank, 1000 m underground in Kamioka mine, Japan
- Neutrinos detection:
 - interaction with electron or nucleus in the water (inverse β decay)
- Instrumented with photomultipliers
 - collects Cherenkov light from (from inverse β decay)
 - Direction of charged particles used to determine **direction of incoming neutrino**
 - Cherenkov rings allow to distinguish e , μ , τ :
 - **Can determine neutrino flavour**



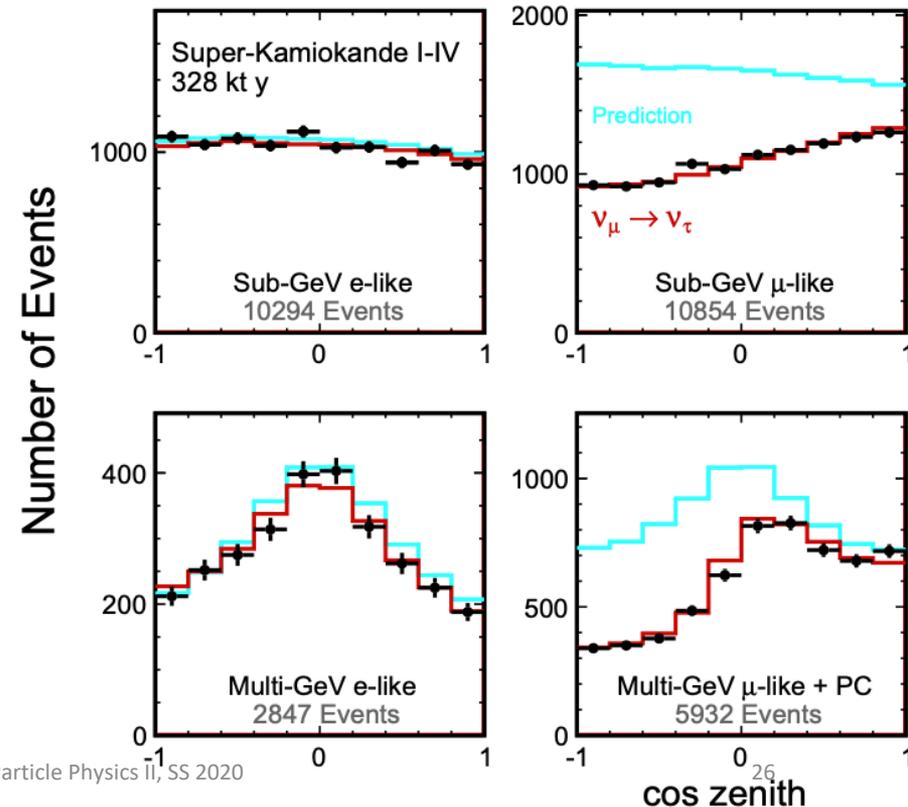
Atmospheric ν oscillations

- Superkamiokande: deficit of ν_μ ($\bar{\nu}_\mu$) with respect to ν_e ($\bar{\nu}_e$) coming from below
 - zenith angle proportional to travel length
- Explained by ν oscillation ($\nu_\mu \rightarrow \nu_\tau$ or $\nu_\mu \rightarrow \nu_e$) while passing through the globe ($L_0 = 10^4$ km)
- Later also measured ν_τ appearance (4.6 σ)
 - Very difficult due to:
 - high threshold for inverse β decay (large τ mass)
 - short τ lifetime



e-like events:
no oscillation

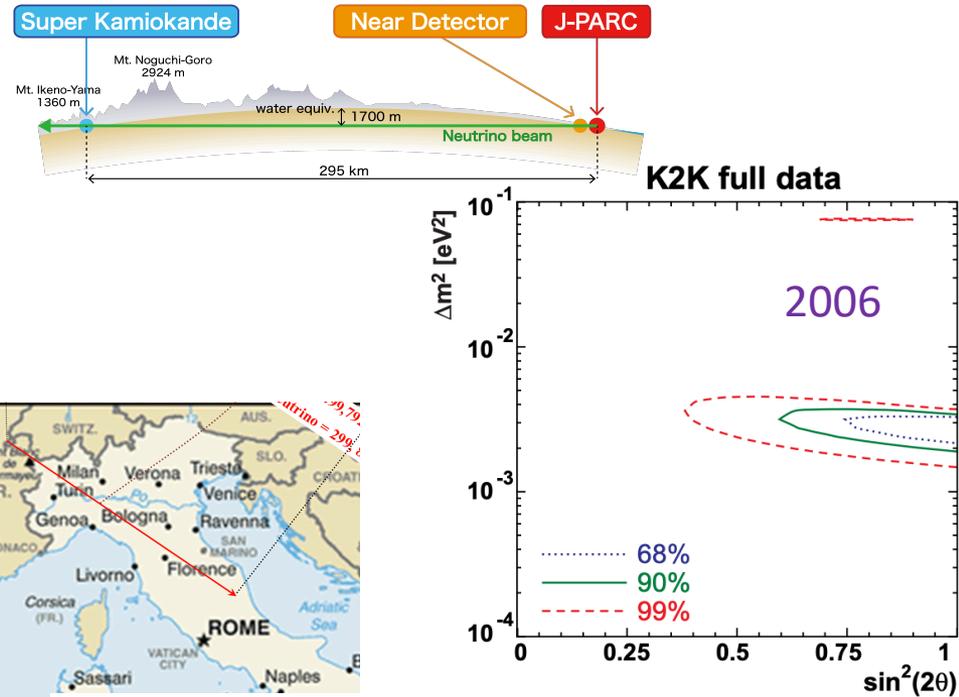
μ -like events:
oscillation observed



Confirmation from long baseline accelerators

○ K2K

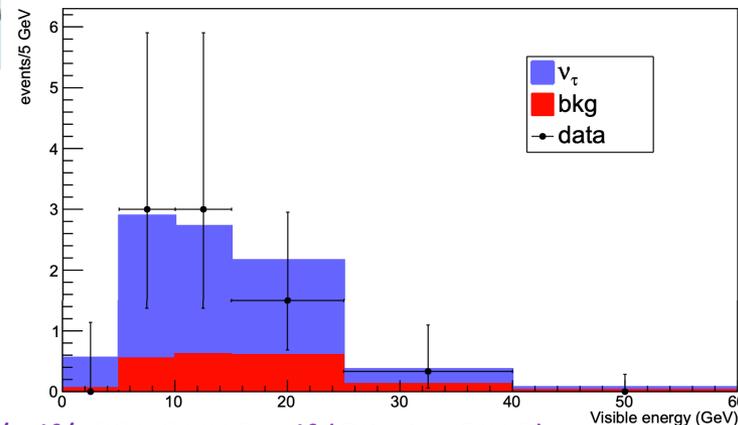
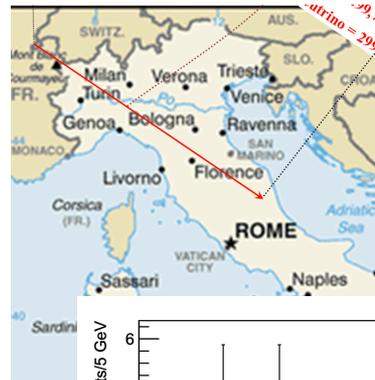
- beam from KEK accelerator to Superkamiokande detector ($L=250$ km)
- First confirmation of ν_μ disappearance outside atmospheric neutrinos (2006)



○ $\nu_\mu \rightarrow \nu_\tau$ appearance confirmed by OPERA

- Beam from CERN to Gran Sasso Laboratories ($L=730$ km)
- Emulsion+lead target

○ $\nu_\mu \rightarrow \nu_e$ appearance observed by MINOS, T2K, NOvA (see later)



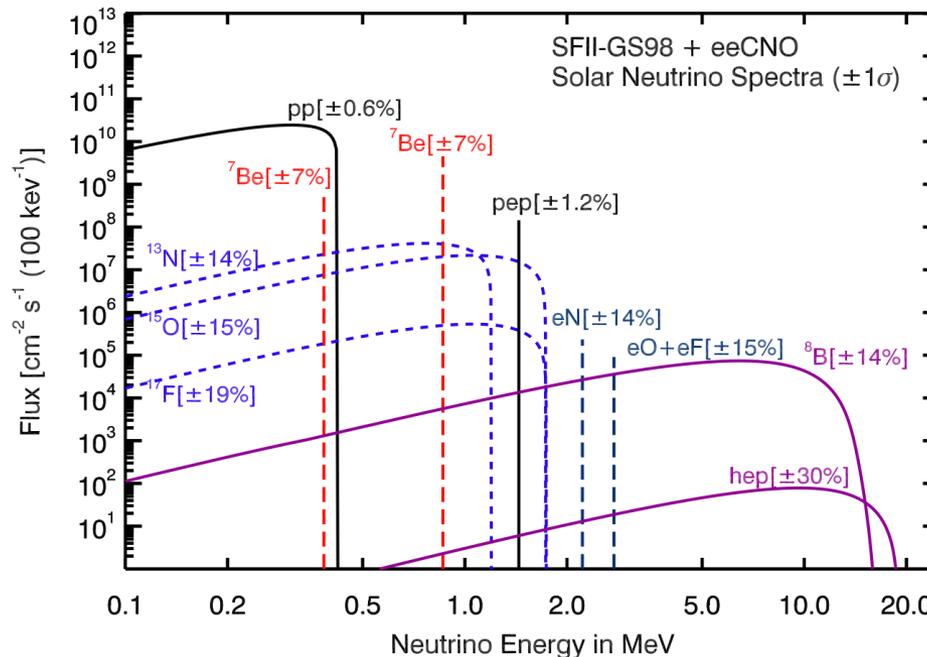
Solar neutrinos

- ν_e produced by thermonuclear fusions in the Sun nucleus
- Solar models predict about 98% of ν produced by the **pp-cycle**
 - It results in:



$$\Rightarrow \langle E_\nu \rangle = 0.59 \text{ MeV}$$

- Remaining 1.6% produced by CNO and Bethe-Weizsäcker cycles



Solar neutrinos

- Two main experimental goals with solar ν

1. Test the Solar Model

- Predicts the temperature distribution in the Sun, which determines the fusion reactions taking place, hence the flux and energy of neutrinos
 - Expected ν flux from the Sun: $1.87 \cdot 10^{38} \text{ s}^{-1}$
 - Expected ν flux density on Earth: $6.6 \cdot 10^{10} \text{ cm}^{-2} \text{ s}^{-1}$
 - ν offer direct, almost instantaneous information about fusion process
 - photons take about 10^6 years to get from the center to the surface, due to strong interaction with solar matter
- Models in good agreement with measured oscillation excitations of the Sun (heliosismology)

2. Search for ν oscillations

- Good search conditions:
 - very low ν energy ($\sim \text{eV}$)
 - very long travel length (10^5 km in Sun matter + 10^8 in vacuum)

$$\implies \Delta m_{\min}^2 \approx \frac{E_\nu [\text{MeV}]}{L [\text{m}]} \text{ eV}^2 \approx 10^{-12} \text{ eV}^2.$$

Solar ν detection

- Two detection methods:
 - 1) Radiochemical measurements
 - 2) Real-time measurements

Table 14.2: List of solar neutrino experiments

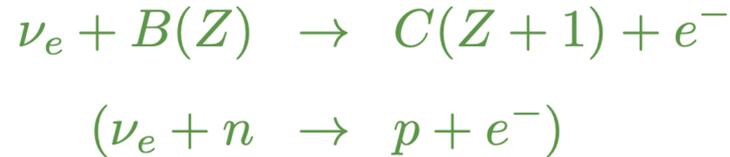
	Name	Target material	Energy threshold (MeV)	Mass (ton)	Years
(1)	Homestake	C ₂ Cl ₄	0.814	615	1970–1994
	SAGE	Ga	0.233	50	1989–
	GALLEX	GaCl ₃	0.233	100 [30.3 for Ga]	1991–1997
	GNO	GaCl ₃	0.233	100 [30.3 for Ga]	1998–2003
(2)	Kamiokande	H ₂ O	6.5	3,000	1987–1995
	Super-Kamiokande (**)	H ₂ O	3.5	50,000	1996–
	SNO	D ₂ O	3.5	1,000	1999–2006
	KamLAND	Liquid scintillator	0.5/5.5	1,000	2001–2007
	Borexino	Liquid scintillator	0.19	300	2007–

From: <http://pdg.lbl.gov/2019/reviews/rpp2019-rev-neutrino-mixing.pdf>

(**) Same detector often works with multiple ν sources

Solar ν detection: radiochemical measurements

- ν captured via inverse β decay of target nuclei



- Detected through decay of the new nuclei C by electron capture
 - Photons or Auger electrons are emitted, which can be detected with a proportional chamber.



- Detector then consists of a huge tank filled with B
 - Targets of choice: Cl^{37} and Ga^{71}
 - ▶ Half life of C must be neither too short nor too long
 - They have different thresholds for ν capture, hence sensitive to different parts of the solar ν spectrum

Solar ν detection: real-time measurements

- Use the reactions

- a) Elastic scattering: $\nu_\alpha e^- \rightarrow \nu_\alpha e^-$

- ▶ The scattered electron indicates the energy and direction of the incident ν (forward scattering)
 - ▶ Used by e.g. (Super-) Kamiokande, SNO, Borexino

- b) ν capture by deuteron (reaction rate 10 times larger than elastic scattering)

- ▶ Two processes:



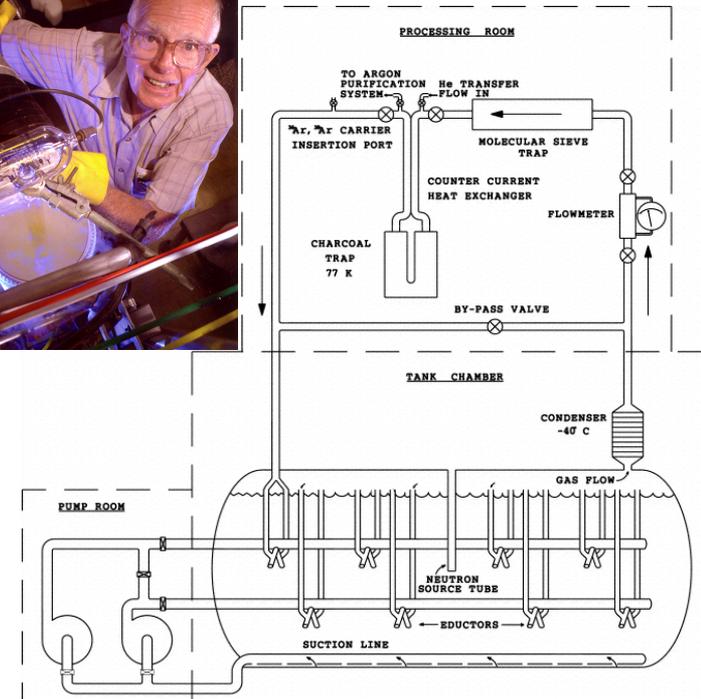
- ▶ By comparing measurements, information on neutrino flux ratio ν_α / ν_e
 - ▶ SNO (Sudbury Neutrino Observatory), Canada: 1000 ton D₂O

The solar ν deficit in summary

- **Homestake** experiment (1970-1994, see next)
 - Using the reaction: $\nu_e + Cl^{37} \rightarrow Ar^{37} + e^-$
 - Found only **$\sim 50\%$ of ν_e expected from Solar Model**
- Confirmed by **SAGE** and **Gallex**
 - Using: $\nu_e + Ga^{71} \rightarrow Ge^{71} + e^-$
 - Different E_ν threshold \rightarrow Different region of the spectrum
- And by **(Super-) Kamiokande**
 - With: $\nu_\alpha e^- \rightarrow \nu_\alpha e^-$
 - $\sigma(\nu_{\mu,\tau} e^-) \approx \frac{1}{6} \cdot \sigma(\nu_e e^-)$
- Explanation: neutrino oscillation in matter (Sun) are different than in vacuum
 - Resonant amplification through the **Mikheyev-Smirnov-Wolfenstein (MSW) effect**: different scattering of ν_e and ν_μ in solar matter with decreasing density
 - 2002 Nobel prize to R. Davis (Homestake) und M. Koshiba (Kamiokande).

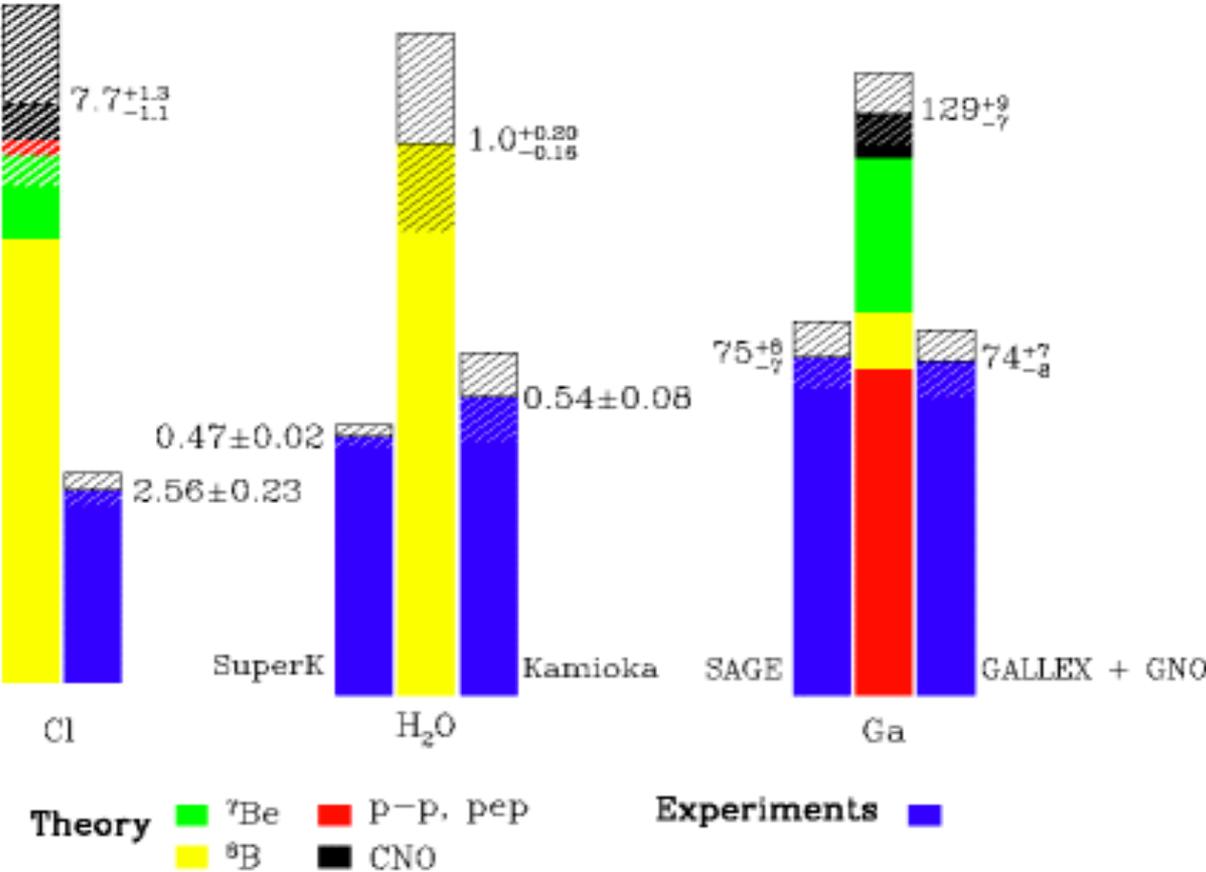
Solar ν deficit: Homestake

- Homestake experiment (R. Davis, Jr. and collaborators)
- About 615 ton of C_2Cl_4
 - In a gold mine in South Dakota
- Method:
 - Exposed for 60-70 days until equilibrium between ν capture and decay (half life: 34.8 days) is reached
 - Chemically extract Ar^{37} (together with known amount of stable Ar^{36}) and introduce it into low-background proportional chamber
 - Reaction rate determined by counting Auger electrons from Ar^{37} decay



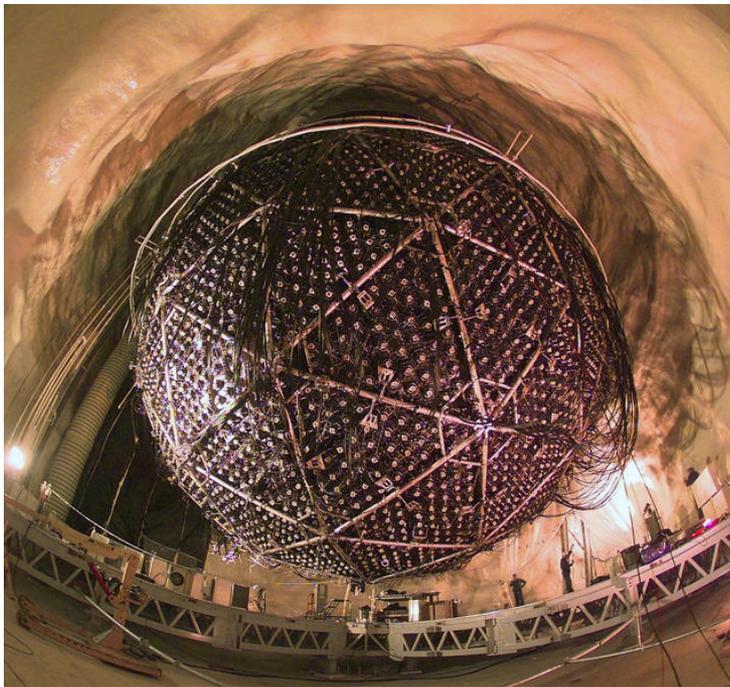
Solar ν deficit: data

Total Rates: Standard Model vs. Experiment
Bahcall-Pinsonneault 2000

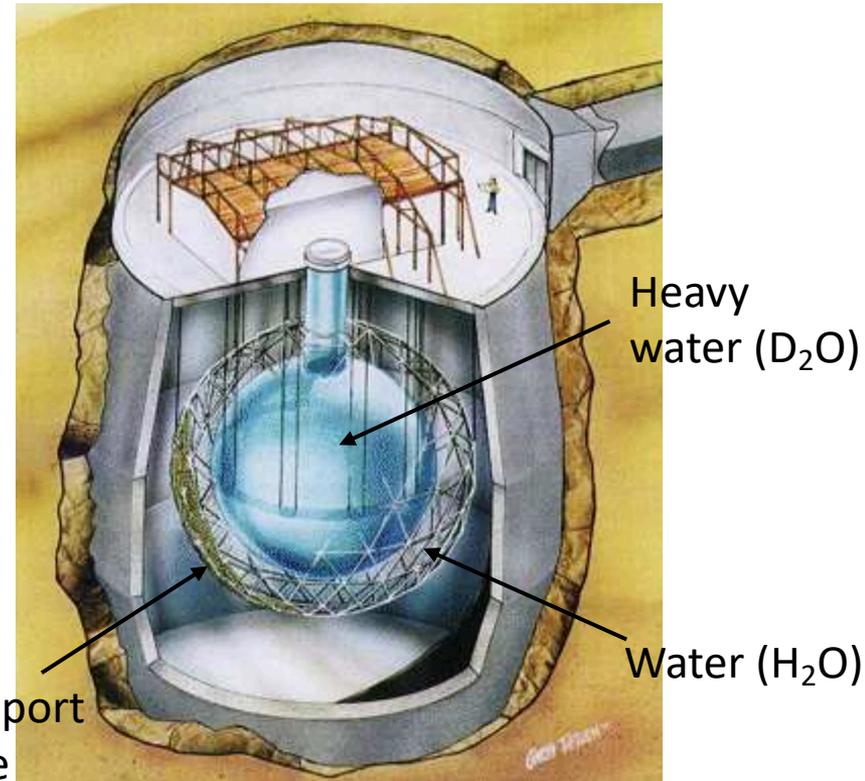


Oscillation hypothesis confirmed by SNO

- SNO (Sudbury Neutrino Observatory), Canada:
 - 1000 ton D_2O in spherical vessel, surrounded by H_2O shield
 - Instrumented with photomultipliers (PMTs) to detect Cherenkov light in both D_2O and H_2O



PMT support structure



Oscillation hypothesis confirmed by SNO

- 3 simultaneous measurements

- ν capture: $\nu_e + d \rightarrow e^- + p + p.$

- only ν_e are detected (charged current)

- deficit is observed

- d spallation: $\nu_\alpha + d \rightarrow \nu_\alpha + p + n$

- all flavours interact with the same cross section

- NO deficit is observed (not sensitive to oscillation)

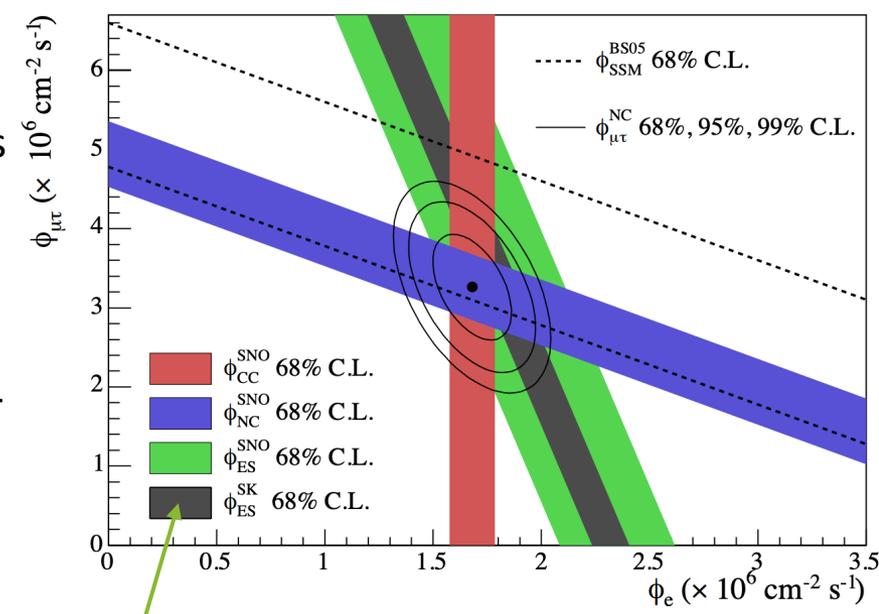
- elastic scattering: $\nu_\alpha e^- \rightarrow \nu_\alpha e^-$

- all flavour interact, but with different cross section ($\sigma_{\nu_e} \sim \frac{1}{6} \sigma_{\nu_\mu + \nu_\tau}$)

- Provides model independent test

- ν_e oscillations confirmed in 2002 by long-baseline reactor experiments (KamLAND, see later)

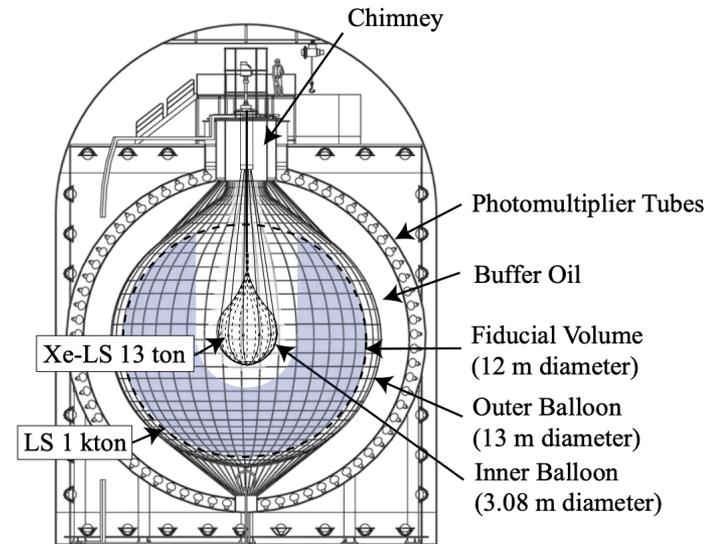
$$\begin{aligned} \Phi_{CC} &= \Phi_e \\ \Phi_{ES} &= \Phi_e + \frac{1}{6} \Phi_{\mu\tau} \\ \Phi_{NC} &= \Phi_e + \Phi_{\mu\tau} \end{aligned}$$



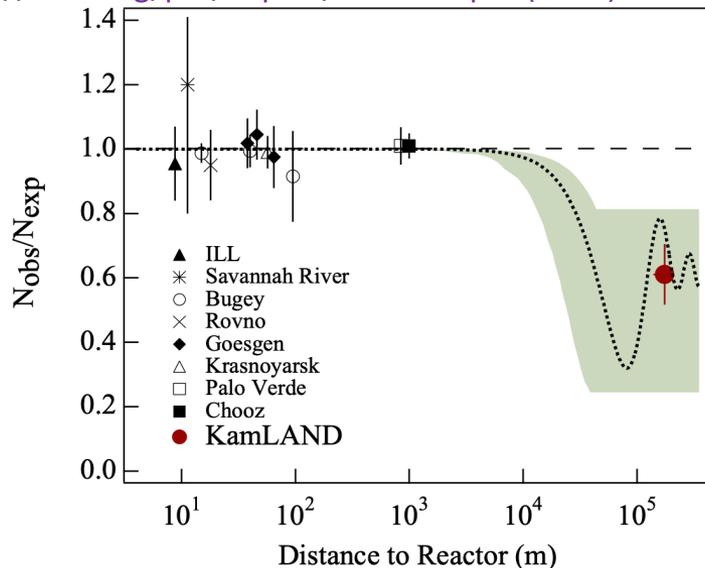
Superkamiokande measurement

Confirmation from reactor neutrino

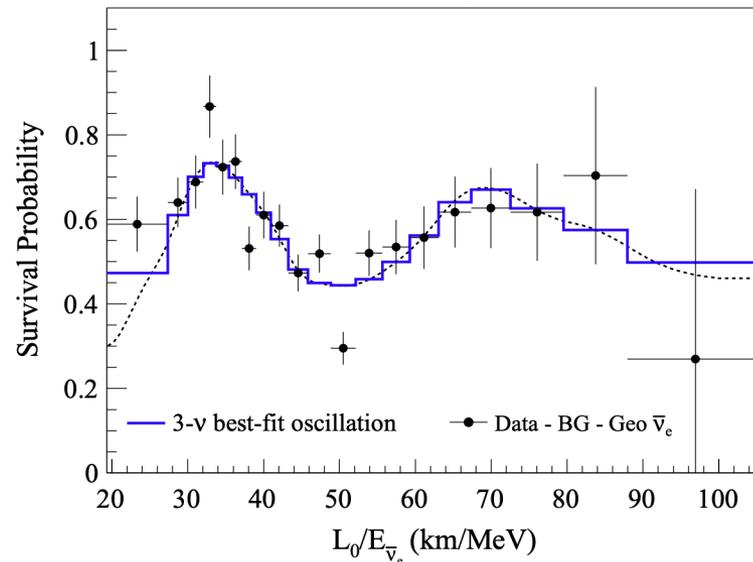
- KamLAND experiment
 - 1000 ton of ultra-pure liquid scintillator in spherical balloon
 - $\bar{\nu}_e$ flux from multiple reactors in Japan and Korea
 - Average distance: 180 km
- In 2002 showed evidence of $\bar{\nu}_e$ disappearance
 - Deficit in agreement with solar model
 - Also in agreement with observations from reactor experiments at shorter distance



<https://arxiv.org/pdf/hep-ex/0212021.pdf> (2002)



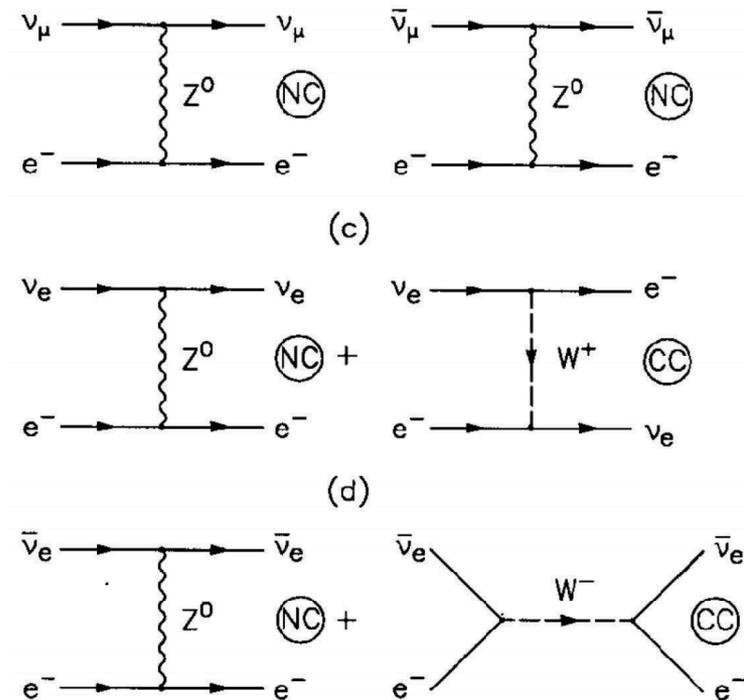
<https://arxiv.org/pdf/1303.4667.pdf> (2013)



Deficit explanation: neutrino oscillation in matter

- Oscillation in matter has different frequency and amplitude than in vacuum
 - First examined by Wolfenstein in 1978
 - Mikheyev and Smirnov, 1985
- Today, the preferred explanation for solar ν deficit

- At low energies, matter is almost transparent to neutrinos
 - Only elastic forward scattering occurs
- Can define an effective refraction index for ν in matter
 - Analog to elastic scattering of light in glass
- Weak interaction with electrons has different cross sections for ν_e and ν_μ/ν_τ
 - Implies different effective refraction indexes: $n_\mu \neq n_e$



ν oscillation in matter: example with two families

- Assuming constant E (constant phase factor in wave function), the free neutrino Hamiltonian is approximately:

$$H = E + \frac{M^2}{2E} \longrightarrow H = \frac{M^2}{2E}.$$

- Taking mixing into account, one can write H as mass operator **in vacuum**.
 - In the mass eigenstate basis:

$$H^{(i)} = \frac{1}{2E} \begin{pmatrix} m_1^2 & 0 \\ 0 & m_2^2 \end{pmatrix}$$

- And in flavour eigenstate basis:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \underbrace{\begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}}_{=U} \cdot \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

$$H^{(\alpha)} = \frac{1}{2E} \begin{pmatrix} m_e^2 & m_{e\mu}^2 \\ m_{e\mu}^2 & m_\mu^2 \end{pmatrix} = U H^{(i)} U^\dagger$$

ν oscillation in matter: example with two families

- Expanding $H^{(\alpha)}$:

$$\begin{aligned} H^{(\alpha)} &= \frac{1}{2E} \begin{pmatrix} m_1^2 \cos^2 \theta + m_2^2 \sin^2 \theta & (m_2^2 - m_1^2) \sin \theta \cos \theta \\ (m_2^2 - m_1^2) \sin \theta \cos \theta & m_1^2 \sin^2 \theta + m_2^2 \cos^2 \theta \end{pmatrix} \\ &\equiv \frac{1}{4E} (m_1^2 + m_2^2) \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \\ &+ \frac{1}{4E} \underbrace{(m_2^2 - m_1^2)}_{=\Delta m^2=:D} \begin{pmatrix} -\cos 2\theta & \sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{pmatrix} \end{aligned}$$

- The mass eigenvalues are then:

$$m_{1,2} = \frac{1}{2} \left[(m_e + m_\mu) \mp \sqrt{(m_\mu - m_e)^2 + 4m_{e\mu}^2} \right]$$

- With:

$$\tan 2\theta = \frac{2m_{e\mu}}{m_\mu - m_e}.$$

ν oscillation in matter: example with two families

- In matter, weak interaction of ν with e adds effective potential to the Hamiltonian
 - Diagonal in flavour states:

$$H \longrightarrow H_m = H + V = \frac{M^2}{2E} + V \quad \Longleftrightarrow$$

$$V_{\alpha\beta}^{(\alpha)} = \langle \nu_\alpha e^- | H_{WW} | \nu_\alpha e^- \rangle \delta_{\alpha\beta},$$

$$V^{(\alpha)} = \begin{pmatrix} V_e & 0 \\ 0 & V_\mu \end{pmatrix}$$

- With global phase transform on the flavour states:

$$|\nu_\alpha\rangle \rightarrow e^{iV_\mu t} |\nu_\alpha\rangle \quad \Rightarrow \quad V^{(\alpha)} = \begin{pmatrix} V_e - V_\mu & 0 \\ 0 & 0 \end{pmatrix} =: \frac{1}{2E} \begin{pmatrix} A & 0 \\ 0 & 0 \end{pmatrix}$$

ν oscillation in matter: example with two families

- The difference between ν_e and ν_μ interaction is due to contribution from charged interaction

$$V_e - V_\mu = \langle \nu_\alpha e^- | H_{WW}^{CC} | \nu_\alpha e^- \rangle \equiv \frac{A}{2E} = \sqrt{2} G_F N_e$$

- With:

$$\begin{aligned} A &= 2\sqrt{2} G_F E N_e = 2\sqrt{2} G_F E \frac{Y_e \rho}{m_N} \\ &= 1.52 \cdot 10^{-7} \cdot E[\text{MeV}] \cdot Y_e \rho [\text{g/cm}^3] \text{ eV}^2 \end{aligned}$$

G_F = Fermi constant for weak $WW = 1.1664 \cdot 10^{-5} \text{ GeV}^{-2}$

$N_e = \frac{Y_e \rho}{m_N}$ = electron density in matter

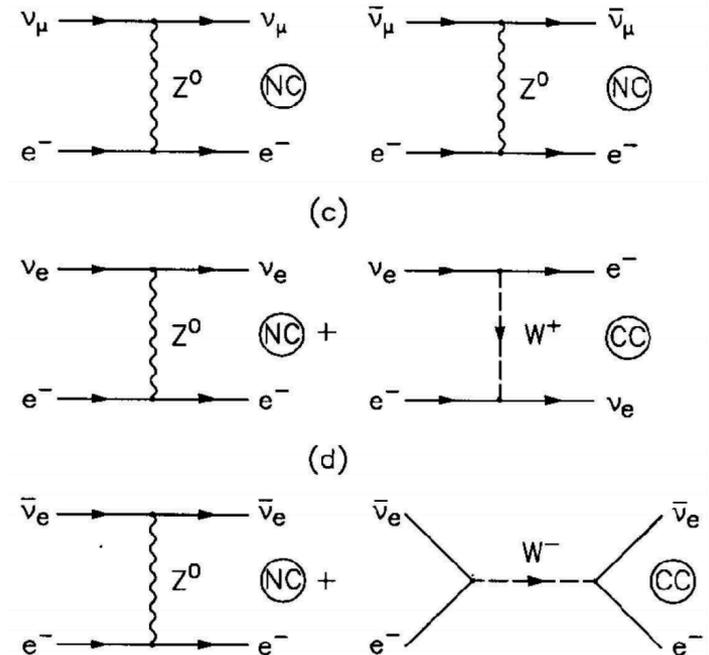
Y_e = number of electrons/nucleons

ρ = matter mass density

m_N = nucleon mass $\approx m_p = 938 \text{ MeV}$

► On average (especially for sun matter)

$$N_e \approx N_p \approx N_n \Rightarrow Y_e \approx \frac{1}{2}$$



ν oscillation in matter: example with two families

- The hamiltonian in matter then becomes
 - For the flavour eigenstates:

$$\begin{aligned} H_m^{(\alpha)} &= H^{(\alpha)} + \frac{1}{2E} \begin{pmatrix} A & 0 \\ 0 & 0 \end{pmatrix} \\ &= \frac{1}{2E} \begin{pmatrix} m_e^2 + A & m_{e\mu}^2 \\ m_{e\mu}^2 & m_\mu^2 \end{pmatrix} \\ &= \frac{1}{4E} (m_1^2 + m_2^2 + A) \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \\ &+ \frac{1}{4E} \begin{pmatrix} A - D \cos 2\theta & D \sin 2\theta \\ D \sin 2\theta & -A + D \cos 2\theta \end{pmatrix} \end{aligned}$$

ν oscillation in matter: example with two families

- The Hamiltonian in vacuum mass eigenstates can then be derived:

$$\begin{aligned} H_m^{(i)} &= U^\dagger H_m^{(\alpha)} U = H^{(i)} + \frac{1}{2E} U^\dagger \begin{pmatrix} A & 0 \\ 0 & 0 \end{pmatrix} U \\ &= \frac{1}{2E} \begin{pmatrix} m_1^2 + A \cos^2 \theta & A \sin \theta \cos \theta \\ A \sin \theta \cos \theta & m_2^2 + A \sin^2 \theta \end{pmatrix}, \end{aligned}$$

- **Not any more diagonal in (ν_1, ν_2)**
 - we now have $\nu_1 \leftrightarrow \nu_2$ transitions due to weak interactions with the matter
 - mass eigenstates in matter: $(\nu_{1m}, \nu_{2m}) \neq (\nu_1, \nu_2)$

ν oscillation in matter: example with two families

- Mass eigenstates in matter: (ν_{1m}, ν_{2m}) obtained by diagonalizing the Hamiltonian operator in the flavour representation

$$U_m^\dagger H_m^{(\alpha)} U_m = H_m^{(i)} = \frac{1}{2E} M_m^{(i)2} := \frac{1}{2E} \begin{pmatrix} m_{1m}^2 & 0 \\ 0 & m_{2m}^2 \end{pmatrix}$$

- Where U_m is the mixing matrix in matter:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \underbrace{\begin{pmatrix} \cos \theta_m & \sin \theta_m \\ -\sin \theta_m & \cos \theta_m \end{pmatrix}}_{=U_m} \cdot \begin{pmatrix} \nu_{1m} \\ \nu_{2m} \end{pmatrix},$$

- One can then compute the mass eigenvalues in matter, as well as the mixing angle θ_m :

$$m_{1,2m}^2 = \frac{1}{2} \left[(m_1^2 + m_2^2 + A) \mp \sqrt{(A - D \cos 2\theta)^2 + D^2 \sin^2 2\theta} \right]$$

$$\tan 2\theta_m(A/D) = \frac{2D \sin 2\theta}{-A + D \cos 2\theta - A + D \cos 2\theta} = \frac{\sin 2\theta}{\cos 2\theta - \frac{A}{D}}$$

ν oscillation in matter: example with two families

- From the expressions for $m_{1,2m}$ and θ_m one can derive the oscillation parameters in matter
 - As a function of those in vacuum

- Mass splitting:

$$D_m \equiv m_{2m}^2 - m_{1m}^2 = D \sqrt{\left(\frac{A}{D} - \cos 2\theta\right)^2 + \sin^2 2\theta} > 0$$

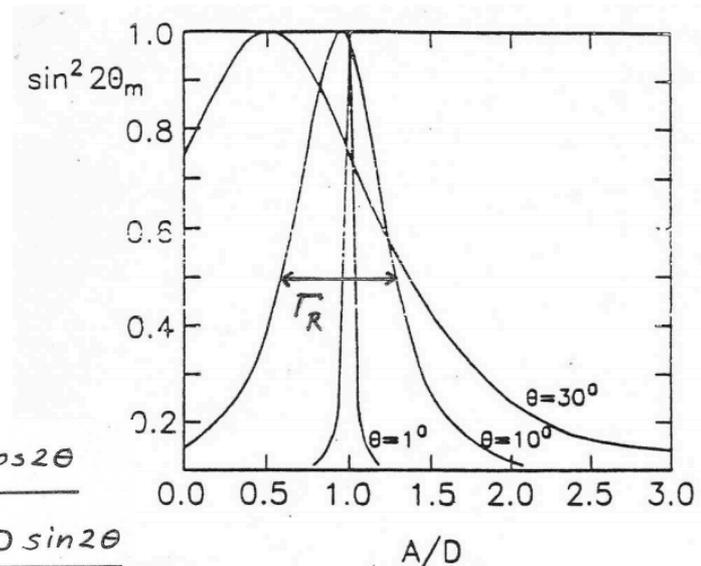
- Oscillation amplitude is a resonance curve as a function of A/D :

$$\sin^2 2\theta_m(A/D) = \frac{\tan^2 2\theta_m}{1 + \tan^2 2\theta_m} =$$

$$= \frac{\sin 2\theta}{\left(\frac{A}{D} - \cos 2\theta\right)^2 + \sin^2 2\theta},$$

$$\left(\frac{A}{D}\right)_R = \cos 2\theta$$

$$\Gamma_R = 2D \sin 2\theta$$



ν oscillation in matter: example with two families

- Survival and transition probabilities then are:

$$\mathcal{P}(\nu_e \rightarrow \nu_e) = 1 - \sin^2 2\theta_m \sin^2 \frac{\Delta_m}{2}$$

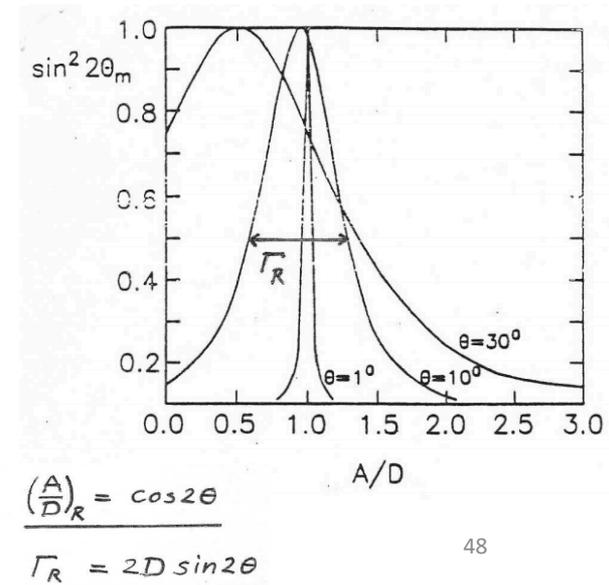
$$\mathcal{P}(\nu_e \rightarrow \nu_\mu) = \sin^2 2\theta_m \sin^2 \frac{\Delta_m}{2}$$

$$\Delta_m := \frac{D_m L}{2 E}$$

- Maximal amplitude for $\theta_m = 45^\circ$
 - Can be reached for any θ , when the A/D ratio is:

$$\frac{A}{D} = \frac{2\sqrt{2}G_F E N_e}{\Delta m^2}$$

- For $\bar{\nu}$: $A \rightarrow -A$
 - Solar neutrinos must be ν and not $\bar{\nu}$

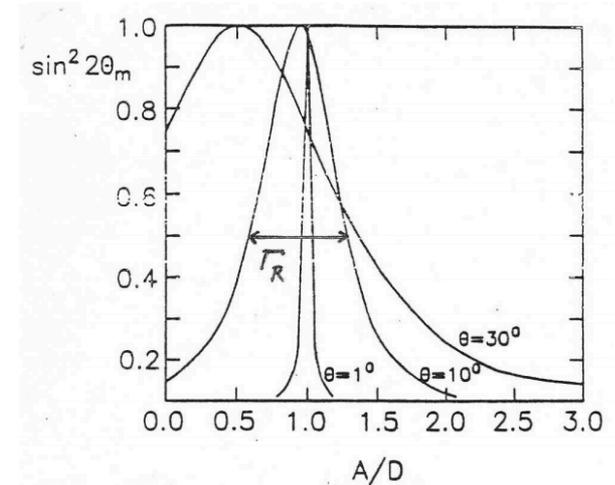


Mikheyev-Smirnov-Wolfenstein Effect

- Resonance in oscillation amplitude, as a function of A/D
 - Depends on density N_e , neutrino energy and vacuum oscillation parameters

- Resonance at:

$$A = A_R = D \cos 2\theta,$$



$$\frac{(A/D)_R}{D} = \cos 2\theta$$

$$\Gamma_R = 2D \sin 2\theta$$

- In the sun, matter density changes along ν path
 - mass eigenstates split as a function of $A \sim N_e$, for given ν energy

- At the sun centre: $\rho = 150 \text{ g/cm}^3$, $Y_e = 0.7$, $N_{e0} = \rho Y_e / m_N$.

- Density then decreases as a function of radius

$$N_e(R) = N_{e0} e^{-10.5R/R_\odot}, \quad R_\odot = 7 \cdot 10^8$$

Mikheyev-Smirnov-Wolfenstein Effect

- 3 regimes

1. Sun nucleus, large N_e : $\frac{A}{D} \gg 1 \Rightarrow A > A_R$

$$\Rightarrow \sin^2 2\theta_m \approx \frac{\sin^2 2\theta}{(A/D)^2} \approx 0$$

$$\Rightarrow \theta_m = 90^\circ$$

$$\Rightarrow D_m \approx A$$

- Oscillation suppressed
- Neutrino states at the source:

$$\begin{aligned} |\nu_{1m}\rangle &\approx -|\nu_\mu\rangle \\ |\nu_{2m}\rangle &\approx |\nu_e\rangle \end{aligned}$$

$$\begin{aligned} m_{1m}^2 &\approx m_2^2 \\ m_{2m}^2 &\approx A \end{aligned}$$

With:

$$m_{1,2m} \approx \frac{1}{2}[m_1^2 + m_2^2 + A \mp (A - D)]$$

$$D = m_2^2 - m_1^2 > 0 \quad A > 0$$

Mikheyev-Smirnov-Wolfenstein Effect

○ 3 regimes

3. Resonance transition during transit through sun

- Continuous density change between 1. and 2.
- At resonance:
 - Amplitude is maximal
 - Mass splitting is maximal

⇒ 'Flavour flip'

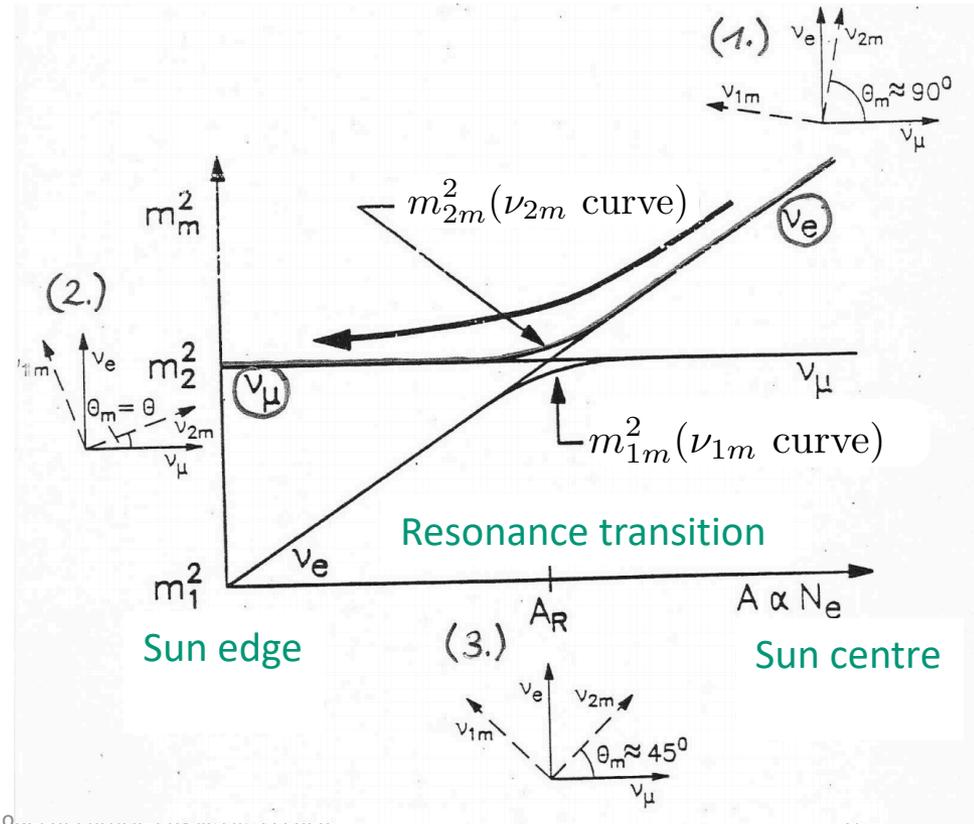
- Neutrino states at resonance:

$$|\nu_{1m}\rangle = \frac{1}{\sqrt{2}}(|\nu_e\rangle + |\nu_\mu\rangle)$$

$$|\nu_{2m}\rangle = \frac{1}{\sqrt{2}}(|\nu_e\rangle - |\nu_\mu\rangle)$$

$$m_{1m}^2 \approx m_{2m}^2$$

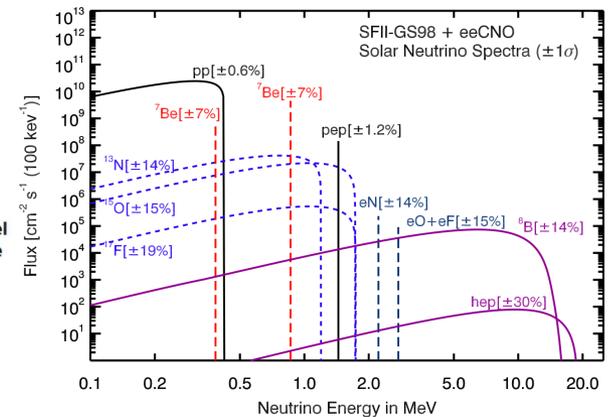
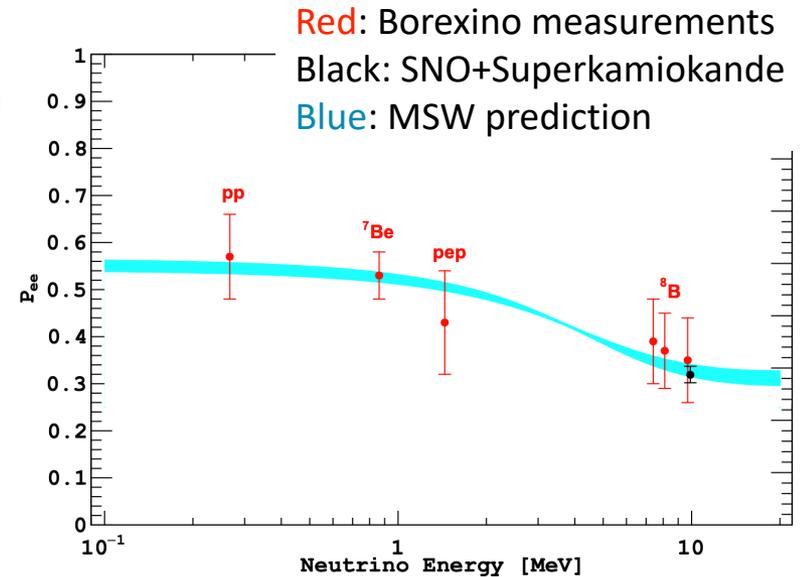
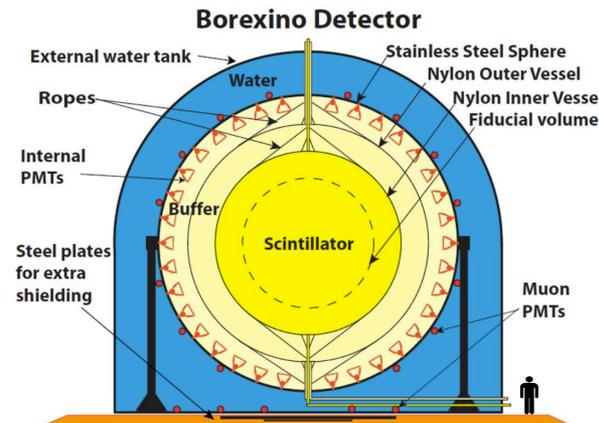
$$m_1^2 \approx m_2^2$$



Deficit explanation: neutrino oscillation in matter

- Observed deficit in solar ν_e consistent with oscillation **in solar matter**.
 - No evidence of further oscillation in vacuum.
- Confirmation with measurements at multiple ν energies by **Borexino** experiment (Gran Sasso Laboratories, Italy)
 - **Borexino**:

- 300 ton of liquid scintillator
- 0.19 MeV energy threshold, 5% energy resolution at 1 MeV
- Allows to distinguish ν from different points of the solar ν spectrum



State of the art: what do we know about neutrinos?

Table 14.6: Experiments contributing to the present determination of the oscillation parameters.

Experiment	Dominant	Important
Solar Experiments	θ_{12}	Δm_{21}^2 , θ_{13}
Reactor LBL (KamLAND)	Δm_{21}^2	θ_{12} , θ_{13}
Reactor MBL (Daya-Bay, Reno, D-Chooz)	θ_{13} , $ \Delta m_{31,32}^2 $	
Atmospheric Experiments (SK, IC-DC)		θ_{23} , $ \Delta m_{31,32}^2 $, θ_{13} , δ_{CP}
Accel LBL $\nu_\mu, \bar{\nu}_\mu$, Disapp (K2K, MINOS, T2K, NO ν A)	$ \Delta m_{31,32}^2 $, θ_{23}	
Accel LBL $\nu_e, \bar{\nu}_e$ App (MINOS, T2K, NO ν A)	δ_{CP}	θ_{13} , θ_{23}

<http://pdg.lbl.gov/2019/reviews/rpp2019-rev-neutrino-mixing.pdf>

ν_μ oscillation

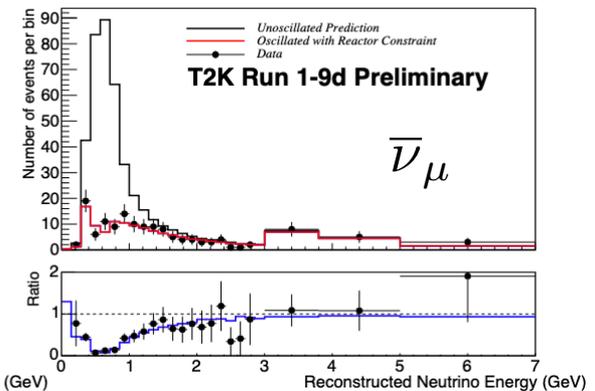
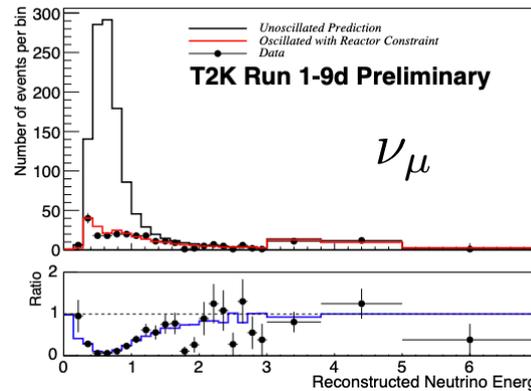
- Atmospheric neutrino:
 - Disappearing ν_μ
 - Appearing ν_τ

- Long baseline accelerator:
 - Disappearing ν_μ
 - Appearing ν_τ
 - Appearing ν_e

Latest long baseline accelerator neutrino experiments

○ T2K (started operations in 2010)

- New high-intensity beam, on Superkamiokande detector
- Tuned on the first maximum of oscillation probability ($\Delta m^2 = 2.5 \cdot 10^{-3} \text{ eV}$)

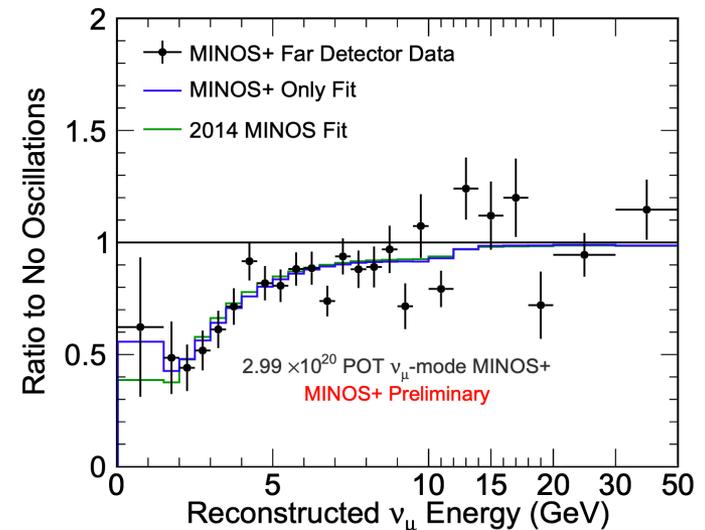


○ MINOS/MINOS+

- beam from Fermilab to Soudan mine ($L=735 \text{ km}$)
- Iron+scintillator tracking calorimeter in magnetic field

○ NOvA (started in 2014)

- beam from Fermilab to Ash River, Minnesota ($L=810 \text{ km}$)
- tracking calorimeter: planes of polyvinyl chloride cells filled with liquid scintillator

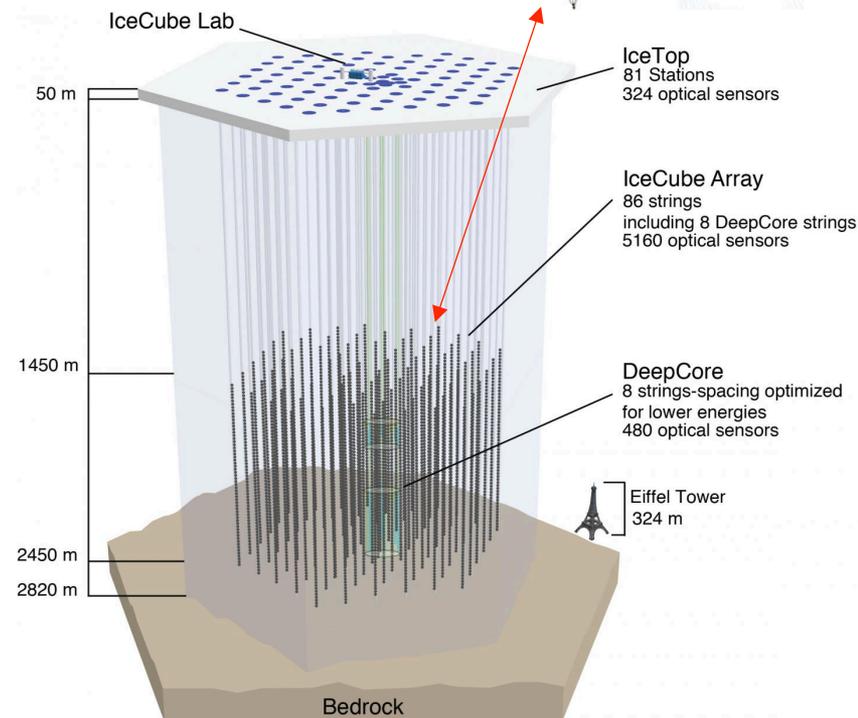
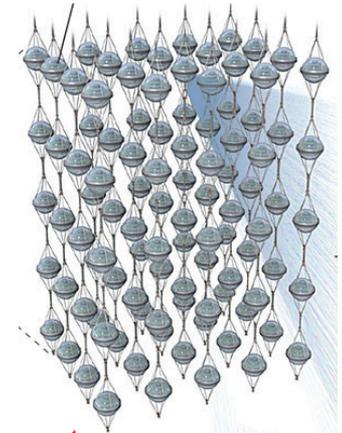


Other atmospheric ν measurements

- Atmospheric ν_μ oscillations confirmed by
 - **MACRO** (Gran Sasso, Italy),
 - **Soudan2** (Soudan Underground Mine, Minnesota)
 - **ANTARES** (Marseille, France) / **IceCube** (South Pole)

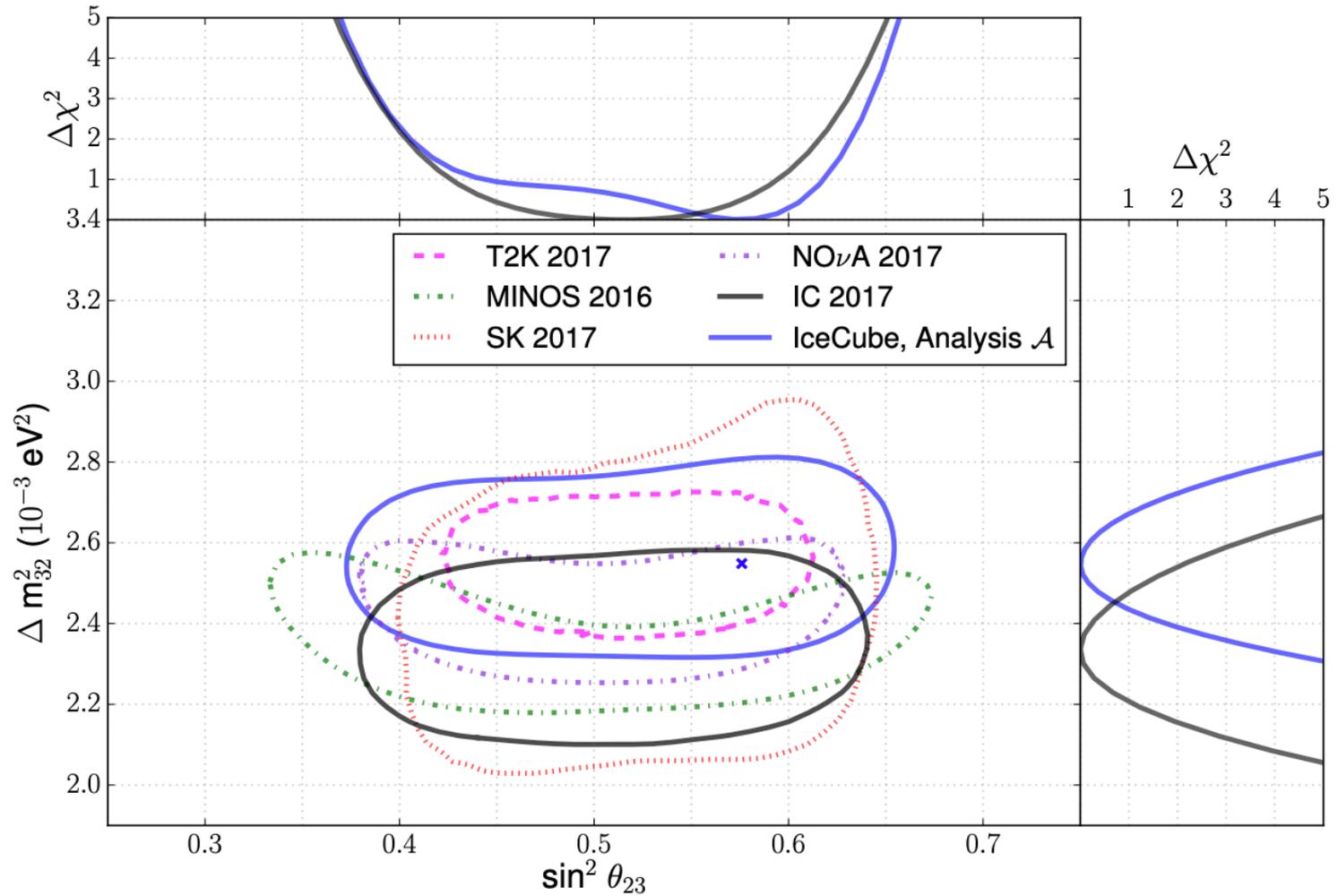
○ ANTARES / IceCube

- Cherenkov detector: strings of photomultipliers inside natural body of water
 - **ANTARES**: in deep Mediterranean sea, near Marseille, France
 - **IceCube** (currently in operation): in polar ice-cap, close to geographical South Pole
- Primarily dedicated to neutrino astronomy
 - neutrinos from supernovas
- Also sensitive to atmospheric neutrinos



Measuring Δm_{23}

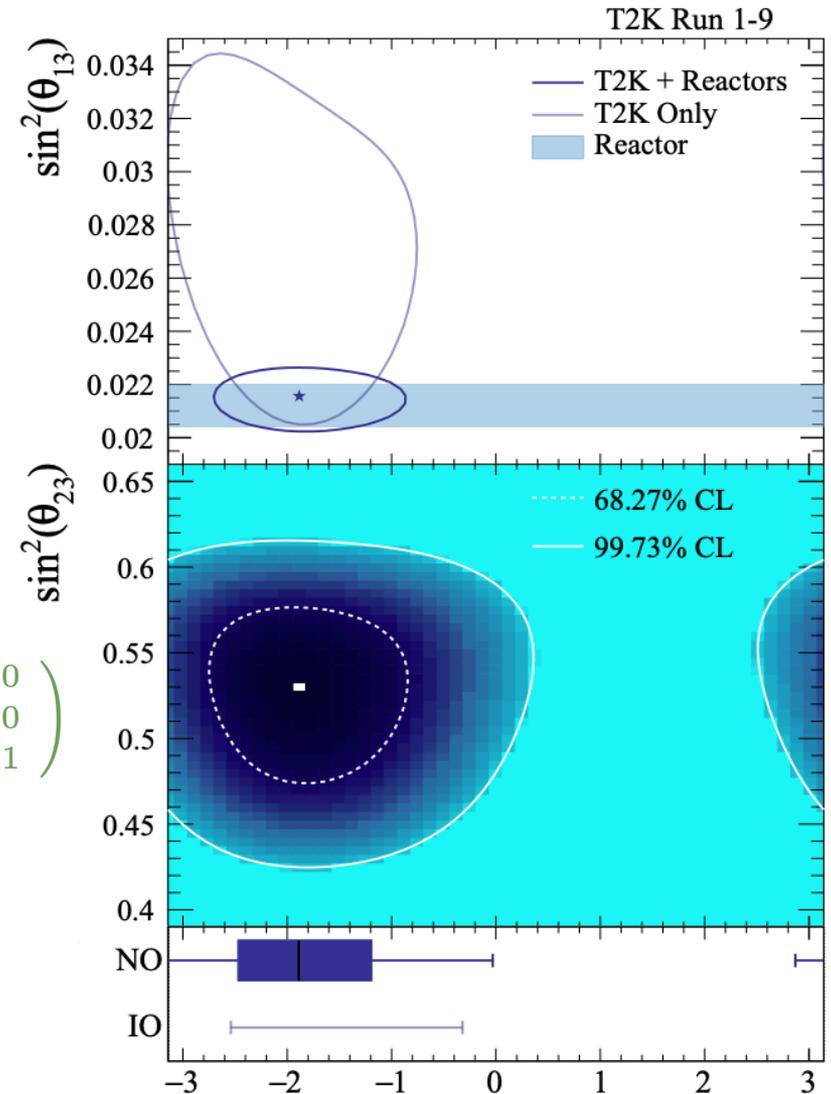
arXiv:1901.05366 [hep-ex] (2019)



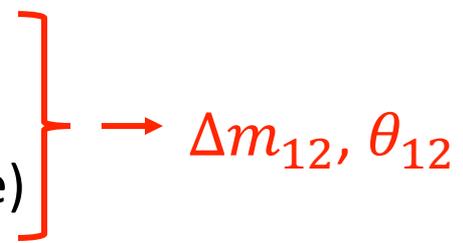
First evidence of CP violations

- T2K:
- 2σ evidence of non-zero δ_{CP}
 - CP-violating phase
- We are starting to probe CP violation in leptons

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} e^{i\phi_1} & 0 & 0 \\ 0 & e^{i\phi_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



ν_e oscillation

- Solar neutrino (discussed before)
 - Long baseline reactors (KamLAND, discussed before)
- 
- $\Delta m_{12}, \theta_{12}$

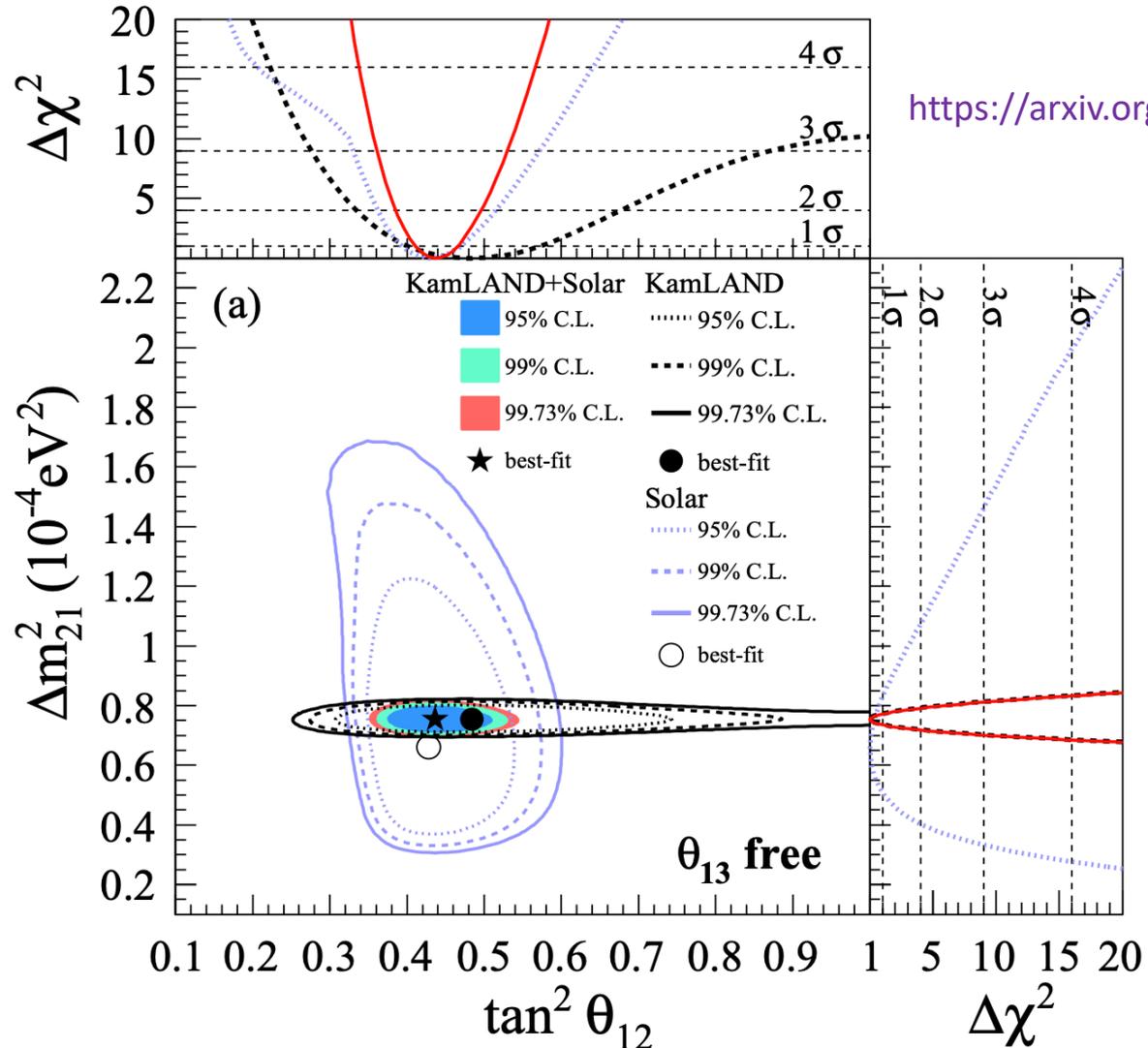
- Medium baseline reactors (Daya-Bay, Reno, D-Chooz: see later)



θ_{13}

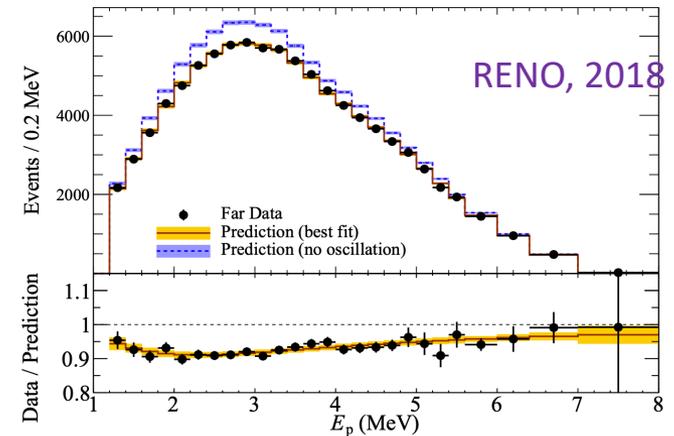
Measuring Δm_{23}

<https://arxiv.org/pdf/1303.4667.pdf>



Measuring θ_{13} : reactor experiments

- $L \sim 1$ km: can measure $\sin^2(2\theta_{13})$ from $\bar{\nu}_e$ disappearance
- First searches in the 90's (CHOOZ, Palo Verde)
- Measurements at **Double CHOOZ**, **Daya-Bay**, **RENO**
 - All started in 2011, first results in 2012
- Double detector (near-far) to go below limits set by previous experiments
 - Double CHOOZ (France): **liquid scintillator**
 - Daya-Bay (China), RENO (Korea): **Cherenkov detector**
- Some $\sim 1\sigma$ tension between the measurements



Double Chooz IV

TnC MD (n-H⊕n-C⊕n-Gd)

$$\sin^2(2\theta_{13}) = 0.105 \pm 0.014$$

Daya Bay

PRL 121,241805(2018) n-Gd

PRD 93,072011 (2016) n-H

$$\sin^2(2\theta_{13}) = 0.086 \pm 0.003$$

$$\sin^2(2\theta_{13}) = 0.071 \pm 0.011$$

RENO

PRL 121,201801(2018) n-Gd

$$\sin^2(2\theta_{13}) = 0.090 \pm 0.007$$

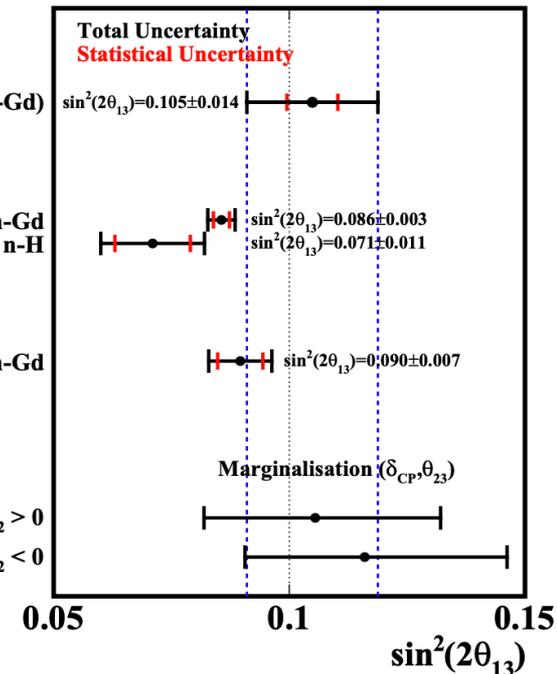
T2K

PRD 96, 092006 (2017)

$$\Delta m_{32}^2 > 0$$

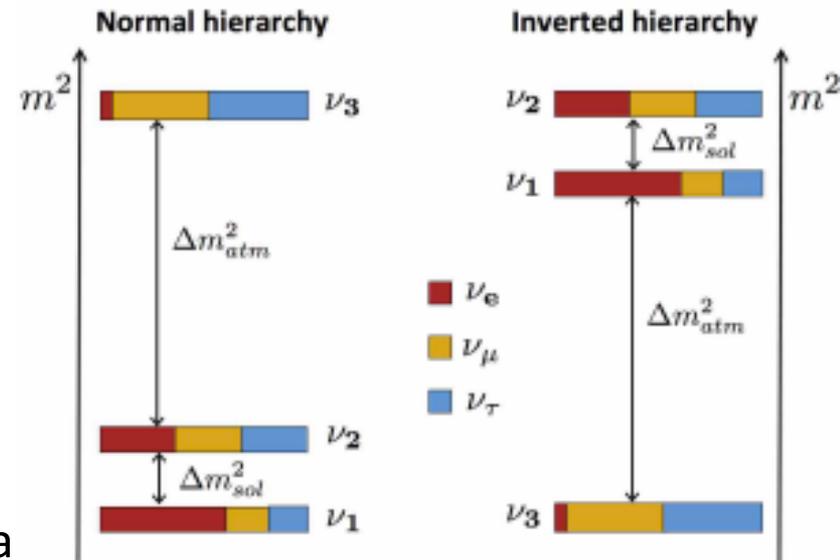
$$\Delta m_{32}^2 < 0$$

Marginalisation (δ_{CP}, θ_{23})



Interpreting the results

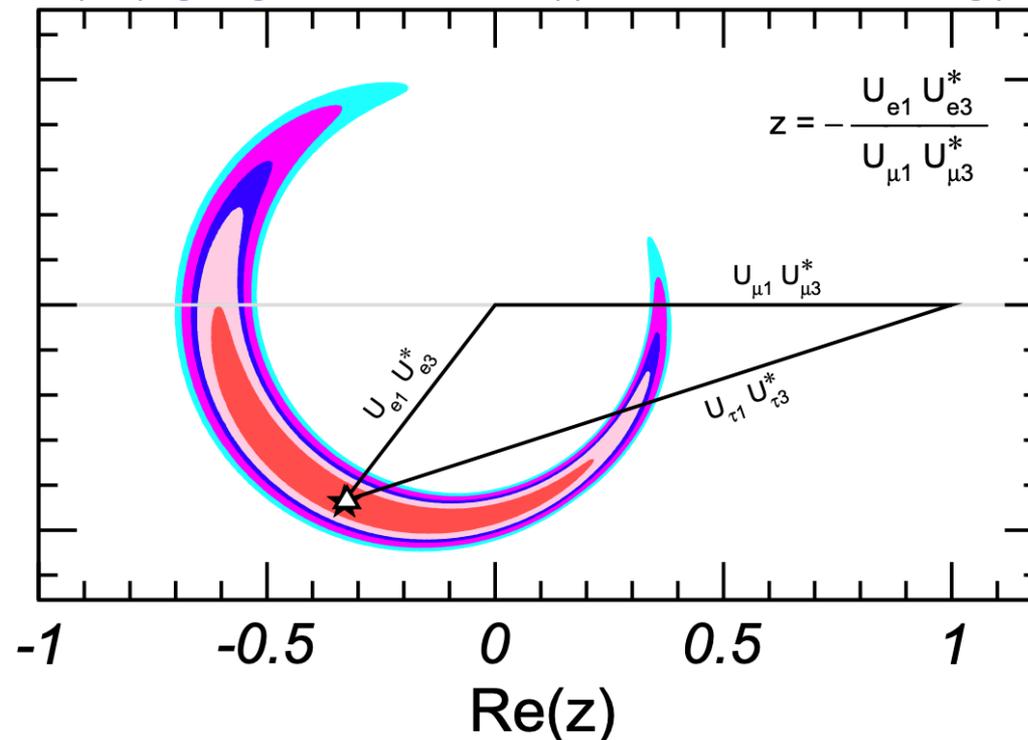
- To fully determine which is the ordering of the 3 mass eigenstates, we need 6 parameters
 - 2 Δm
 - 3 mixing angles
 - 1 CP phase
- Experiments in general are in agreement with one another
- Two scenarios compatible with the data we have
 - Normal hierarchy vs Inverted hierarchy
- We are missing (or not known with enough precision): θ_{23}, δ_{CP}



Interpreting the results: leptonic unitarity triangle

- Results available can be used to build a ‘leptonic unitarity triangle’, in the same way as for the quarks
 - Hints at nonzero area: CP violation occurs
 - But still compatible with CP conservation within 1-2 σ

<http://pdg.lbl.gov/2019/reviews/rpp2019-rev-neutrino-mixing.pdf> (2019)



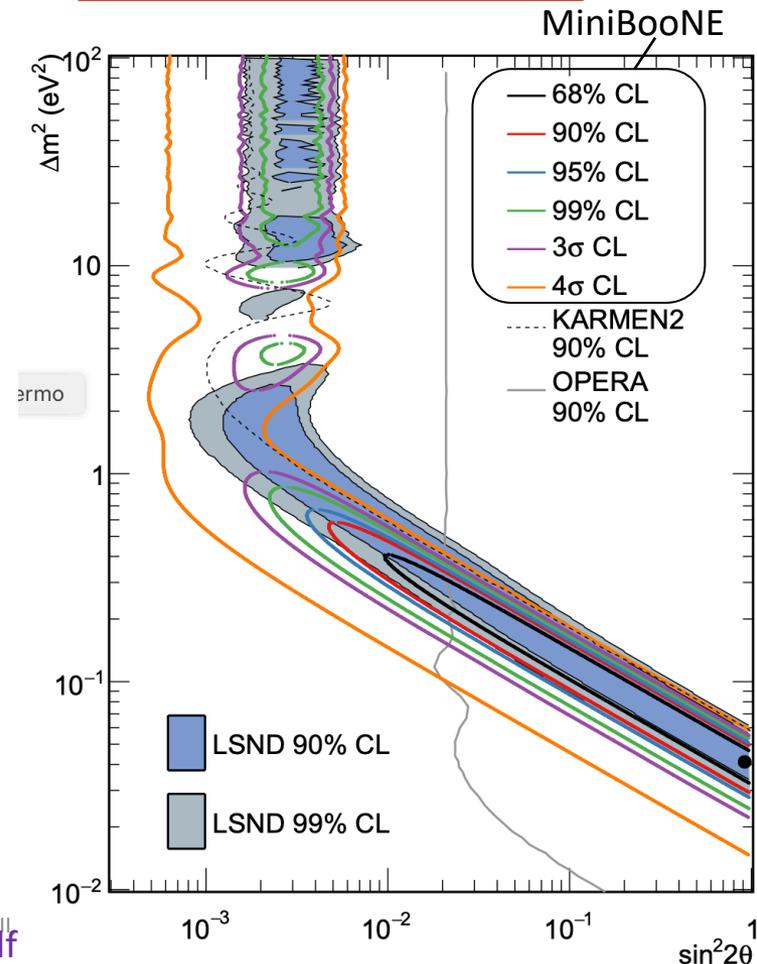
Anomalies: short distance $\nu_\mu \rightarrow \nu_e$

- **LSND** experiment: ν from 780 MeV p-LINAC at Los Alamos ($L=30$ m)
 - Search for $\nu_\mu \rightarrow \nu_e$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_e$) oscillation
 - Observed **excess compatible with $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$** appearance
- **KARMEN** experiment: ν from 800 MeV proton accelerator at RAL, London ($L=28$ m)
 - No $\bar{\nu}_e$ excess observed, **excludes** parameter area favoured by LSND
- **MiniBooNE**: ν from Fermilab Booster beamline
 - Same parameter region as LSND
 - Observes both ν_e and $\bar{\nu}_e$ **excess at 4.7σ**
- **To be further investigated** with multi-detector experiments (in preparation)
 - LSND and MiniBooNE were single-detector experiments
 - e.g.
 - SBN program, Fermilab
 - JSNS² experiment, JPARK (Japan)

Note:

- T2K: $L/E \sim 500$ m/MeV
- Here: $L/E \sim 1$ m/MeV

Not the same effect!



- Neutrino oscillation still a quite open field
- Vast variety of new experiment planned for upcoming years

Neutrino mass direct measurements

- Neutrino oscillation can only tell the **difference** between neutrino masses
- For the **absolute scale**, a direct measurement is needed
- ν_e : measure end point of e energy spectrum from tritium β decay (see later)
- ν_μ : muon pulse measurement in weak π decay (PSI, Zürich) $\pi^+ \rightarrow \mu^+ \nu_\mu$
 - masses of μ and π known very well from energy levels of pionic atoms and muon magnetic moment

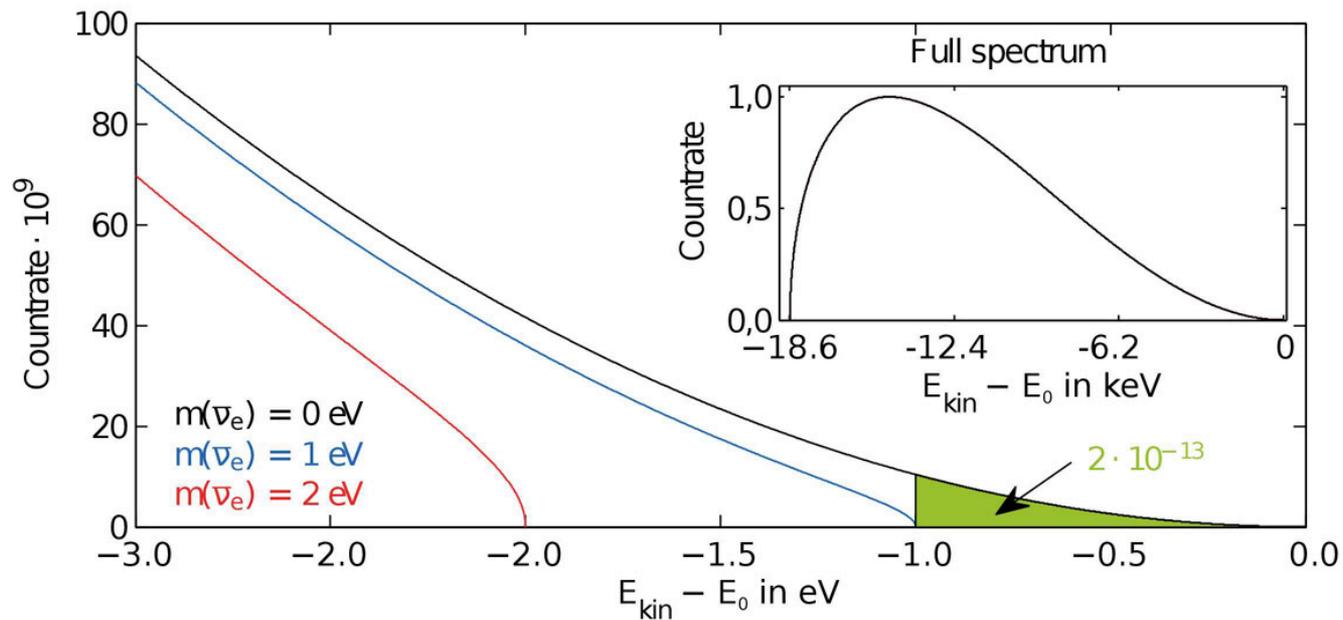
$$\sum_i m_i |U_{\mu i}|^2 < 190 \text{ keV},$$

- ν_τ : end point of hadron invariant mass in hadronic τ decays:
$$m_{\nu_\tau} = m_\tau - \text{Max}(m_{\text{Hadronen}})$$
 - m_τ known precisely from e^+e^- storage rings (BES, Beijing)
 - Best results from ALEPH, at LEP

$$\sum_i m_i |U_{\tau i}|^2 < 18.2 \text{ MeV}.$$

ν_e mass measurement

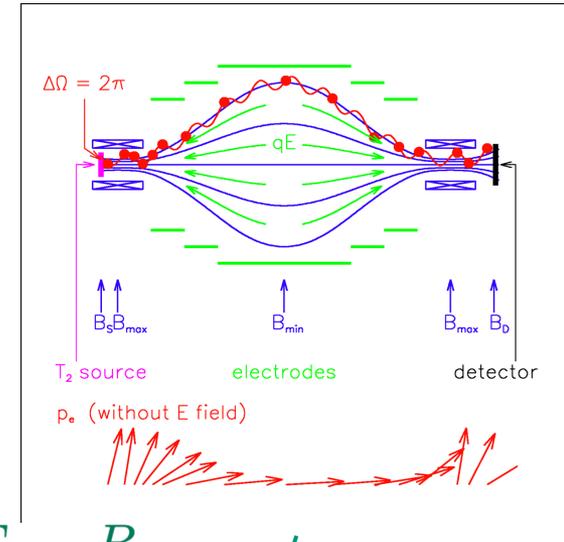
- Measure end point of e energy spectrum from tritium β decay



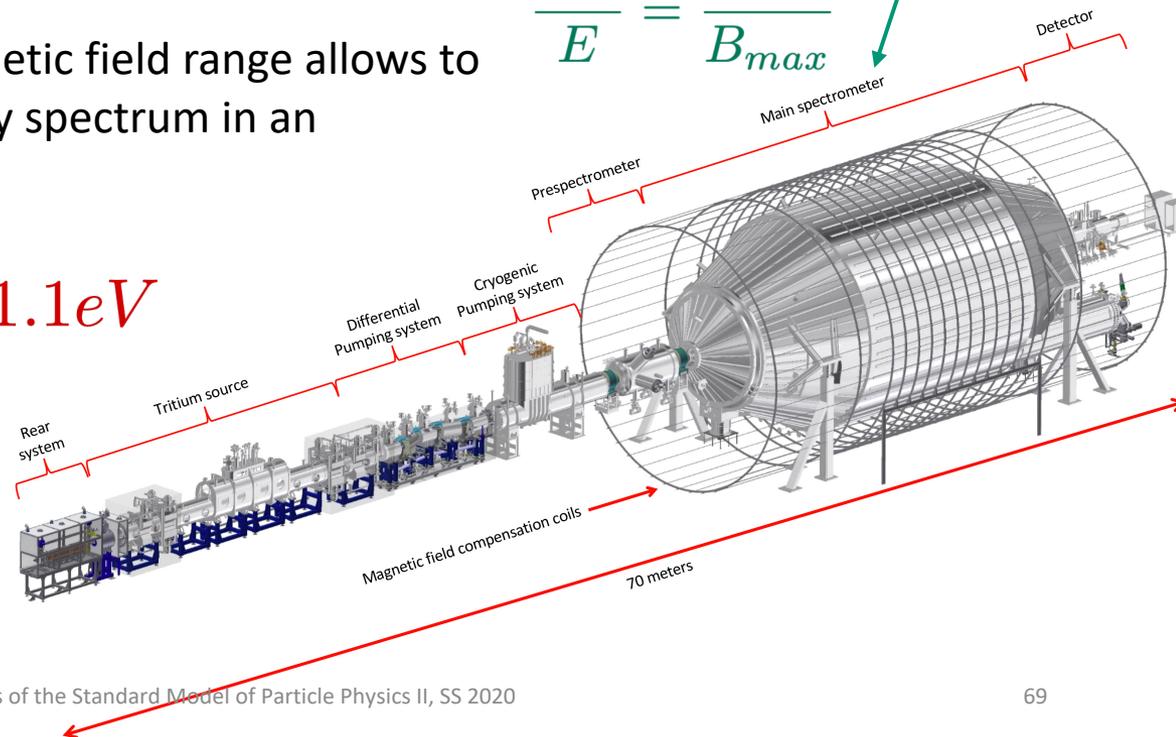
ν_e mass measurement

- Magnet spectrometers:
 - First experiments: Mainz, Troitsk
 - Best limit from KATRIN experiment (Karlsruhe)
 - Magnetic field selects only electrons with high enough energy
 - By varying the magnetic field range allows to measure the β decay spectrum in an integrating mode

$$\sum_i m_i |U_{ei}|^2 < 1.1 \text{ eV}$$



$$\frac{\Delta E}{E} = \frac{B_{min}}{B_{max}}$$

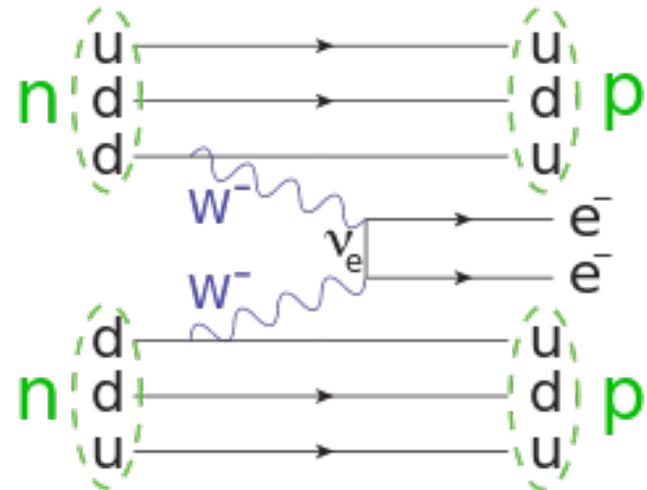


Majorana neutrinos?

- If neutrinos are (massive) Majorana particles ($\bar{\nu} = \nu$)
 - Neutrinoless double β decay must occur
 - Half life proportional to ν mass squared
- Signature: sum of electron energies equal to Q -value from nuclear transition
 - Ultra-low background experiments, large source mass needed

$$T_{1/2}^{0\nu} \sim | \langle m_{ee} \rangle |^2$$

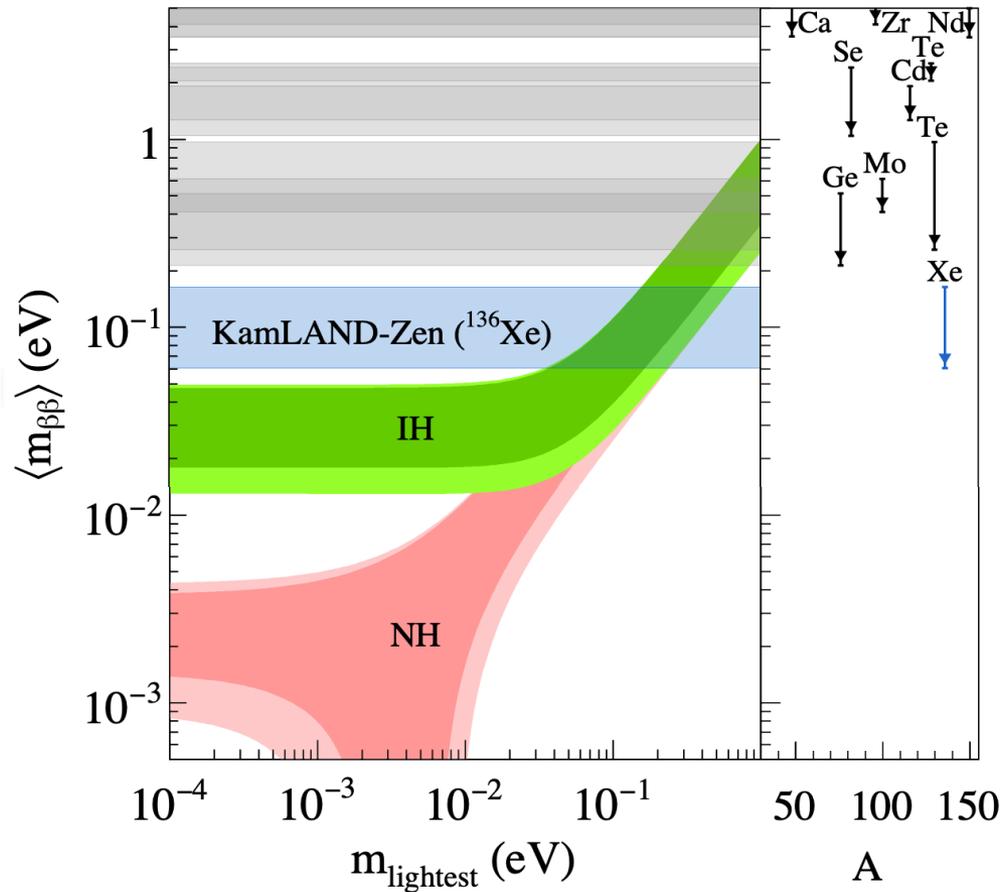
$$\langle m_{ee} \rangle = \sum_i m_i U_{ei}^2$$



Majorana neutrinos?

- Multiple techniques used
- Ultra-pure Germanium detector (ionization detector)
 - Enriched in ^{76}Ge
 - GERDA, Majorana demonstrator
- Liquid scintillator detector: use existing detector, by adding β source
 - KamLAND-Zen: add balloon with Xenon enriched in ^{136}Xe
 - Currently gets the strongest bound: $T_{1/2}^{0\nu} > 1.07 \times 10^{26}$
 - SNO+: similar idea
- Other experiments (some, in preparation) use time projection chambers, or bolometric detectors

ν_e mass: results summary



IH: inverted hierarchy
 NH: normal hierarchy